

宇宙論の諸問題(仮)

Inflation, dark energy, dark matter, ...

Shuichiro Yokoyama (KMI, Nagoya Univ.)

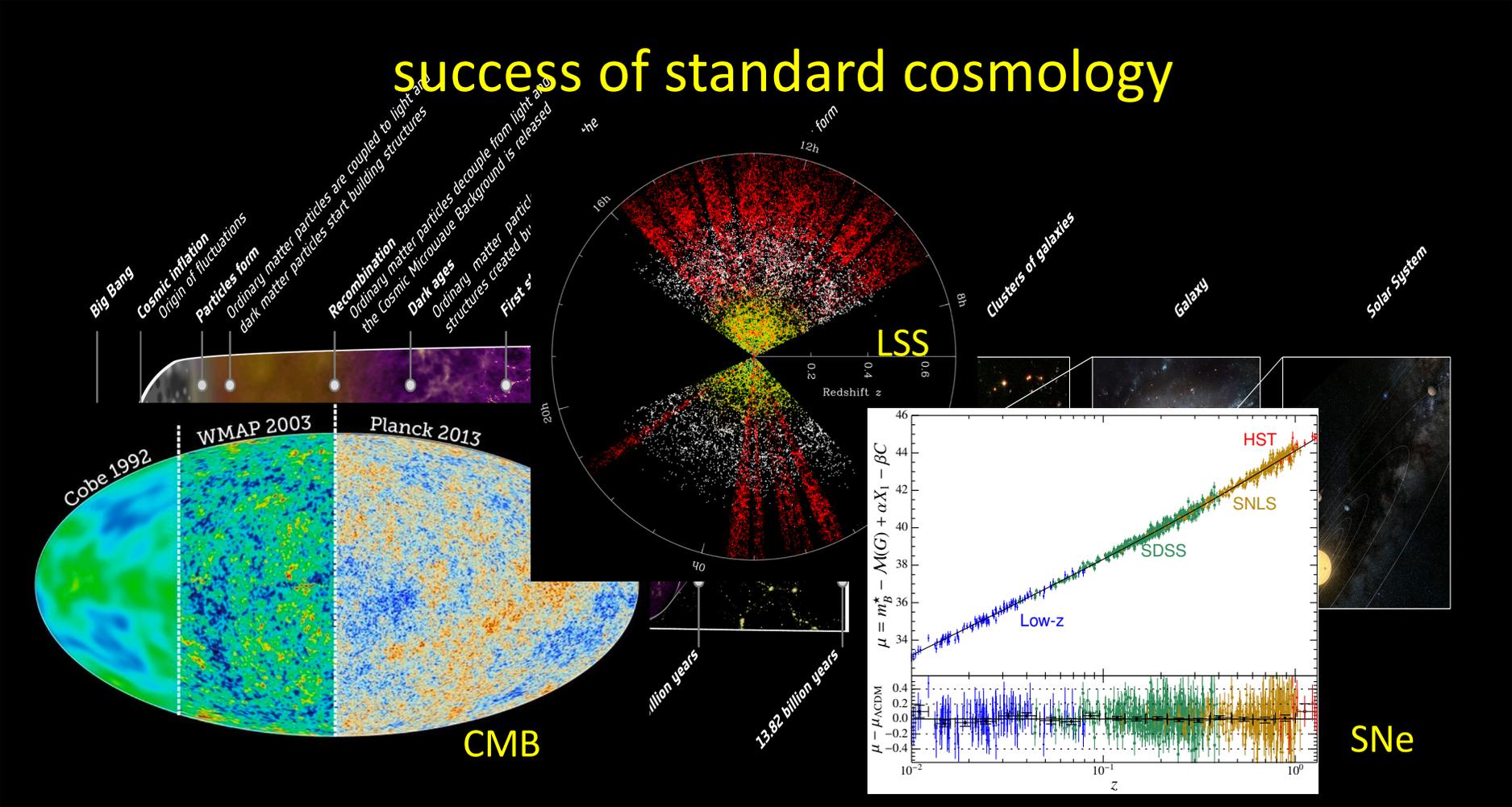
「第5回銀河進化と遠方宇宙」2019

contents

- Overview
- Inflation
- Dark energy
- Dark matter
- Summary

Overview

success of standard cosmology



Overview

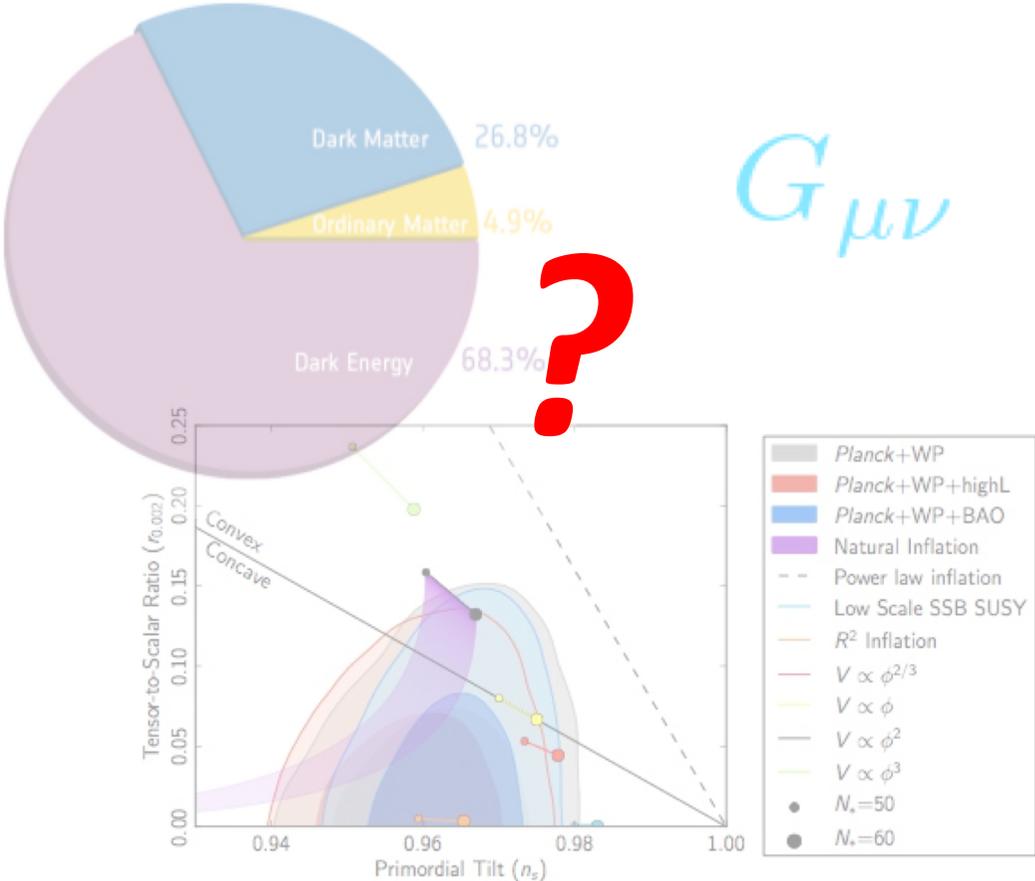
- Standard component in cosmology

Standard Model of Elementary Particles

	three generations of matter (fermions)			interactions / force carriers (bosons)	
	I	II	III		
mass	$\approx 2.2 \text{ MeV}/c^2$	$\approx 1.28 \text{ GeV}/c^2$	$\approx 173.1 \text{ GeV}/c^2$	0	$\approx 125.09 \text{ GeV}/c^2$
charge	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0	0
spin	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	0
QUARKS	u up	c charm	t top	g gluon	H higgs
	$\approx 4.7 \text{ MeV}/c^2$	$\approx 96 \text{ MeV}/c^2$	$\approx 4.18 \text{ GeV}/c^2$	0	
	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	0	
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	
	d down	s strange	b bottom	γ photon	
	$\approx 0.511 \text{ MeV}/c^2$	$\approx 105.66 \text{ MeV}/c^2$	$\approx 1.7768 \text{ GeV}/c^2$	$\approx 91.19 \text{ GeV}/c^2$	
	-1	-1	-1	0	
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	
LEPTONS	e electron	μ muon	τ tau	Z Z boson	
	$< 2.2 \text{ eV}/c^2$	$< 1.7 \text{ MeV}/c^2$	$< 15.5 \text{ MeV}/c^2$	$\approx 80.39 \text{ GeV}/c^2$	
	0	0	0	± 1	
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	
	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	W W boson	

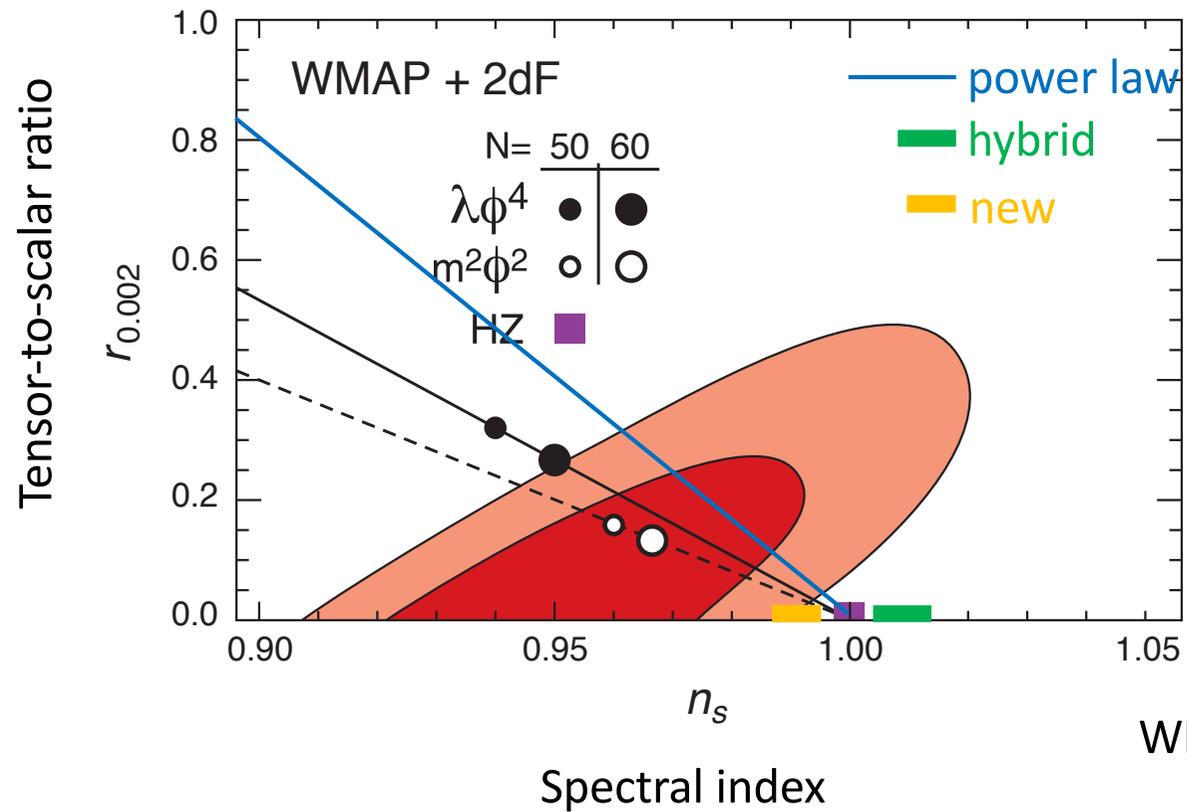
SCALAR BOSONS (Higgs)
GAUGE BOSONS VECTOR BOSONS (photon, Z, W)

Any others?

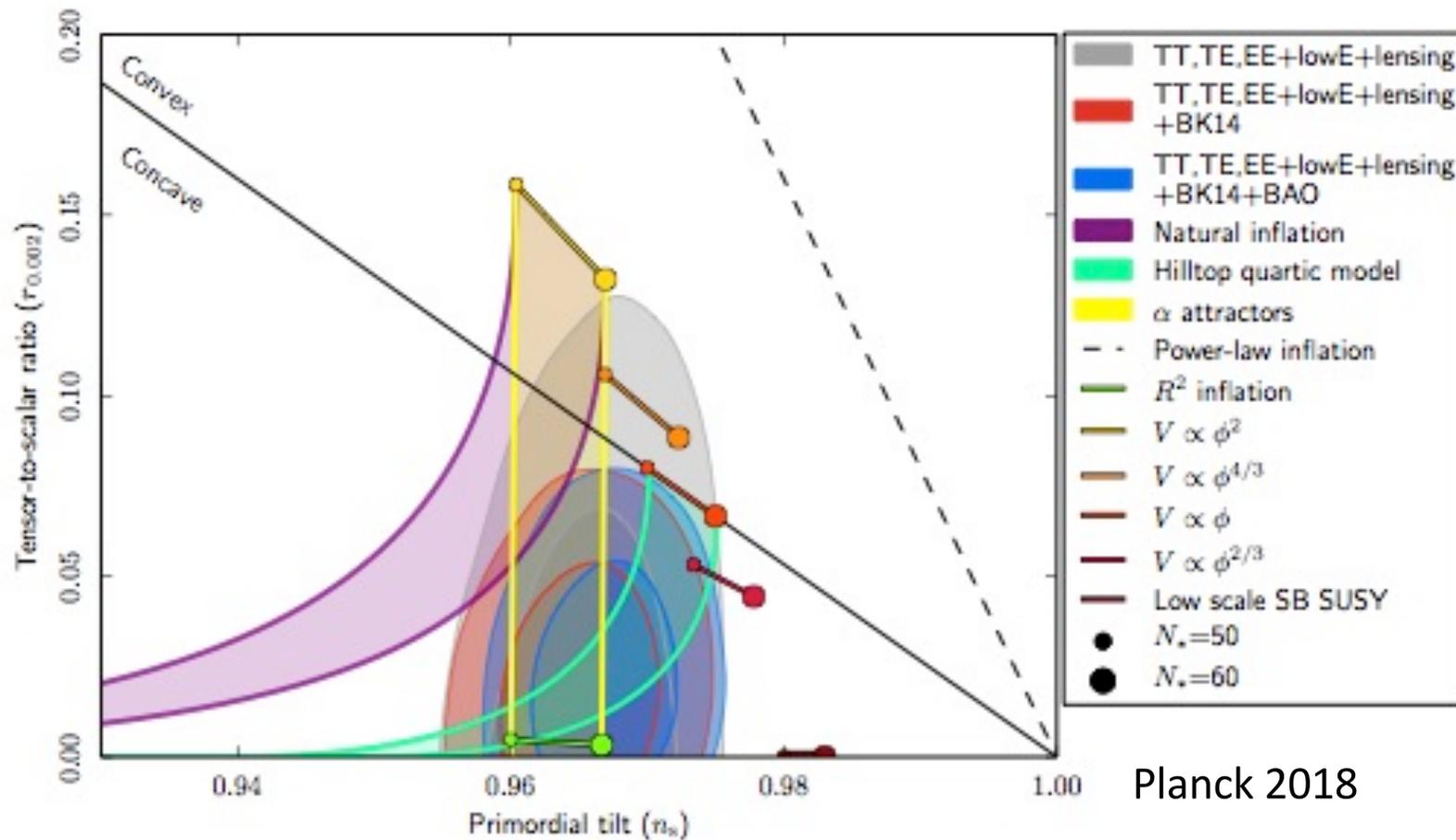


inflation

Constraint on CMB



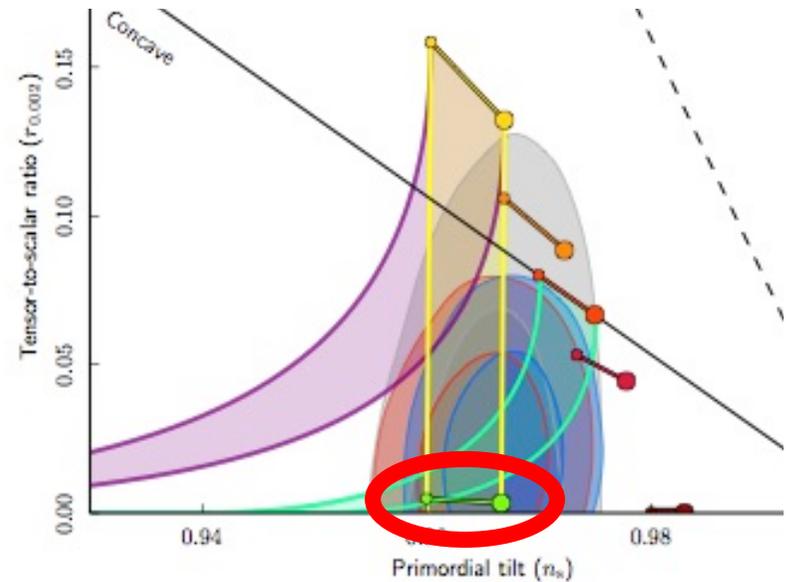
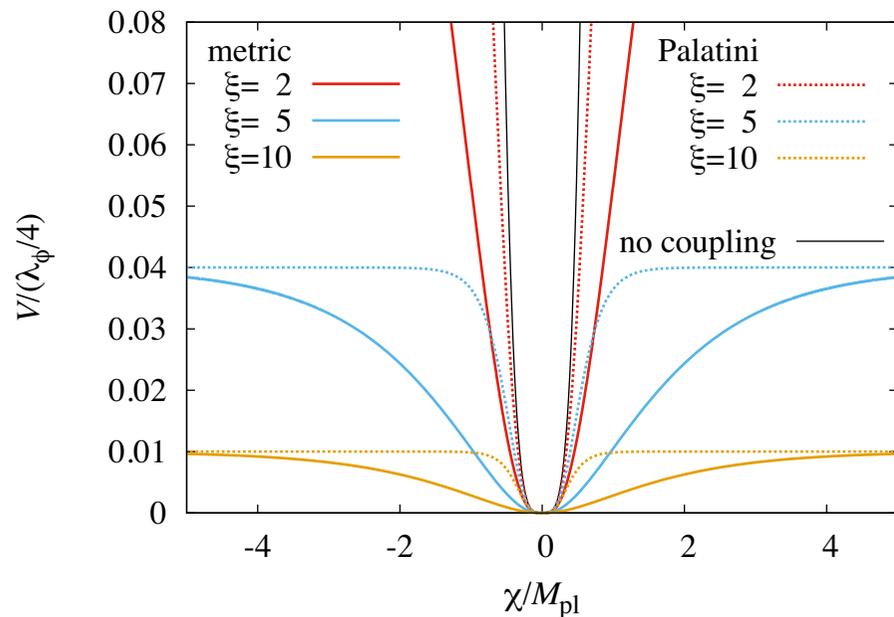
Constraint on CMB



Beyond standard??

Inflaton with a non-minimal coupling

$$\lambda\phi^4 \text{ with } \xi\phi^2 R,$$



Best model?

Takahashi, Tenkanen(2018)

↔ Starobinsky model (R^2 inflation)

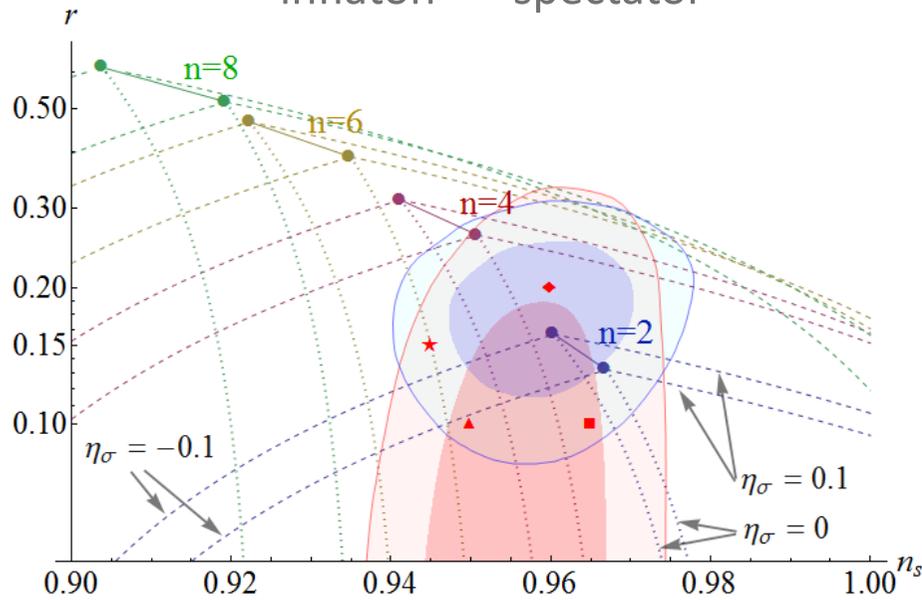
$$\delta T/T \sim 10^{-5} \implies \frac{\xi}{\sqrt{\lambda}} \simeq 47000$$

(Higgs inflation, Bezrukov, Shaposhnikov (2008))

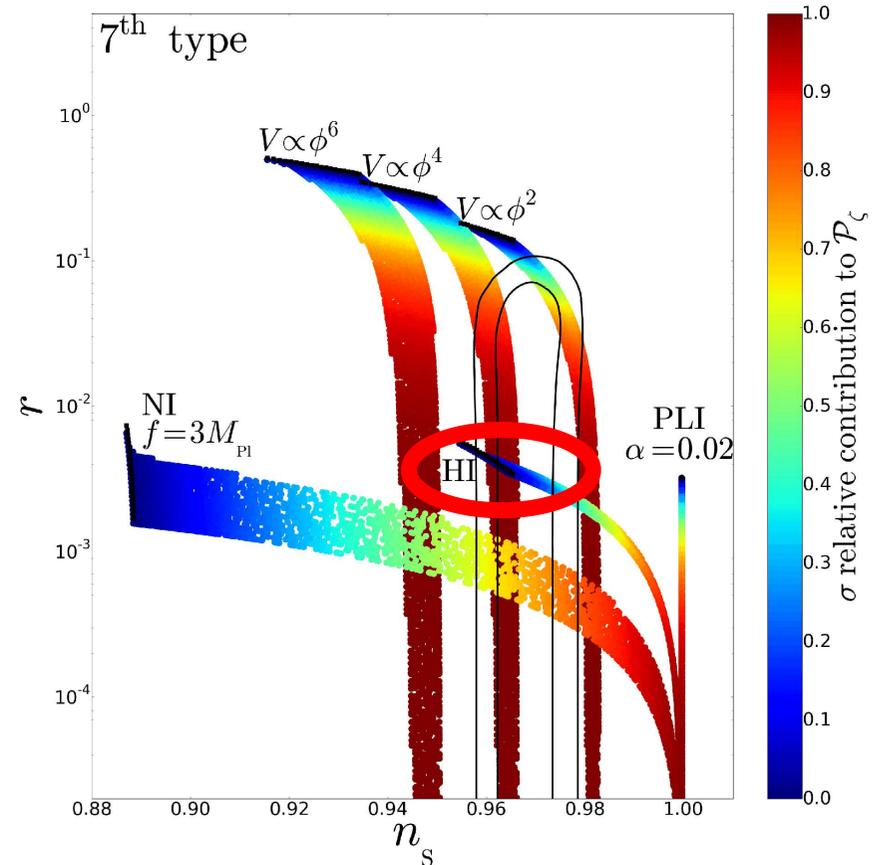
Inflaton with a spectator field - extension to multi-field case -

$$\mathcal{P}_s(k) = \mathcal{P}_s^{(\phi)}(k) + \mathcal{P}_s^{(\chi)}(k),$$

inflaton spectator



Fujita, Kawasaki, SY (2014)



“Encyclopædia curvatonis”

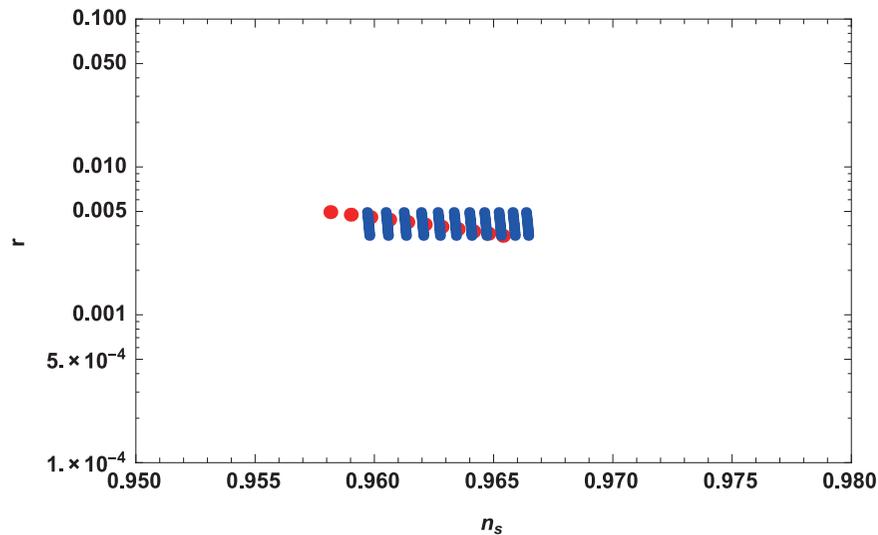
Vennin, Koyama, Wands (2015)

Not only tensor-to-scalar ratio, but also spectral index should change

→ degenerate ?

R² inflation and ...

Nariai and Tomita (1971), Starobinsky (1980), ...

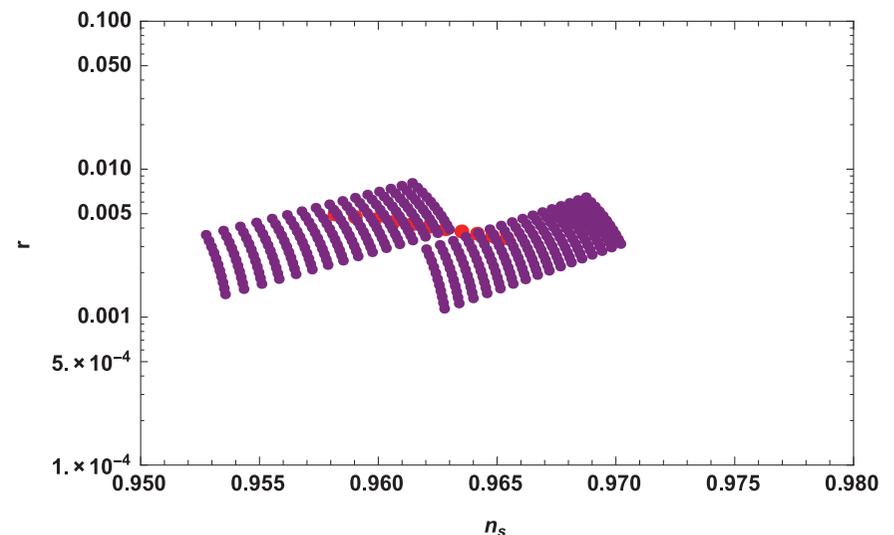


R² inflation (N = 50 - 60)

phi⁴-inflation with a massless spectator
(N = 50 - 60)

$r = (1 - Q_\chi)16\epsilon$; tensor-to-scalar ratio

$$Q_\chi \equiv \frac{\mathcal{P}_s^{(\chi)}(k_0)}{\mathcal{P}_s^{(\phi)}(k_0) + \mathcal{P}_s^{(\chi)}(k_0)}$$



natural inflation with a massless spectator
(N = 50 - 60, $Q_\chi = 0.5, 0.6$,
 $f = 3.3 - 3.75 M_{\text{pl}}$)

$$V(\phi) = \Lambda^4 \left[1 - \cos \frac{\phi}{f} \right]$$

Sekiguchi, Takahashi, Tashiro, SY in preparation

How to discriminate?

- Higher order ?

Local type non-Gaussianity in multi-scalar inflation

$$\zeta = \zeta_G + \frac{3}{5} f_{\text{NL}} (\zeta_G^2 - \langle \zeta_G^2 \rangle) + \dots$$

Linear perturbation (free propagation) \leftrightarrow Gaussian

- \rightarrow through the non-linear interaction
- \rightarrow non-zero higher order perturbations
- \rightarrow non-Gaussianity!!
- \rightarrow observed by higher order correlation functions!

Standard single slow-roll case; $\zeta \sim \frac{V}{V_\phi} \delta\phi + \underbrace{\left(\frac{V_\phi^2}{V^2} - \frac{V_{\phi\phi}}{V} \right)}_{\text{slow-roll suppressed!!}} \left(\frac{V}{V_\phi} \delta\phi \right)^2$

Spectator case; $\zeta \sim F \frac{\delta\rho_\sigma}{\rho_\sigma} \sim F \frac{\delta\sigma}{\sigma} + \frac{1}{F} \left(F \frac{\delta\sigma}{\sigma} \right)^2$
 $(\rho_\sigma \propto \sigma^2)$

transfer from spectator to curvature perturbations

Distinguishing models by Local type NG

- Single inflation vs spectator (curvaton, ...)

Critical value; $f_{\text{NL}}^{\text{local}} = O(0.1 - 1)$

Spectator (curvaton) scenario $\rightarrow f_{\text{NL}}^{\text{local}} > O(1)$

due to the transfer from spectator to adiabatic curvature pert.

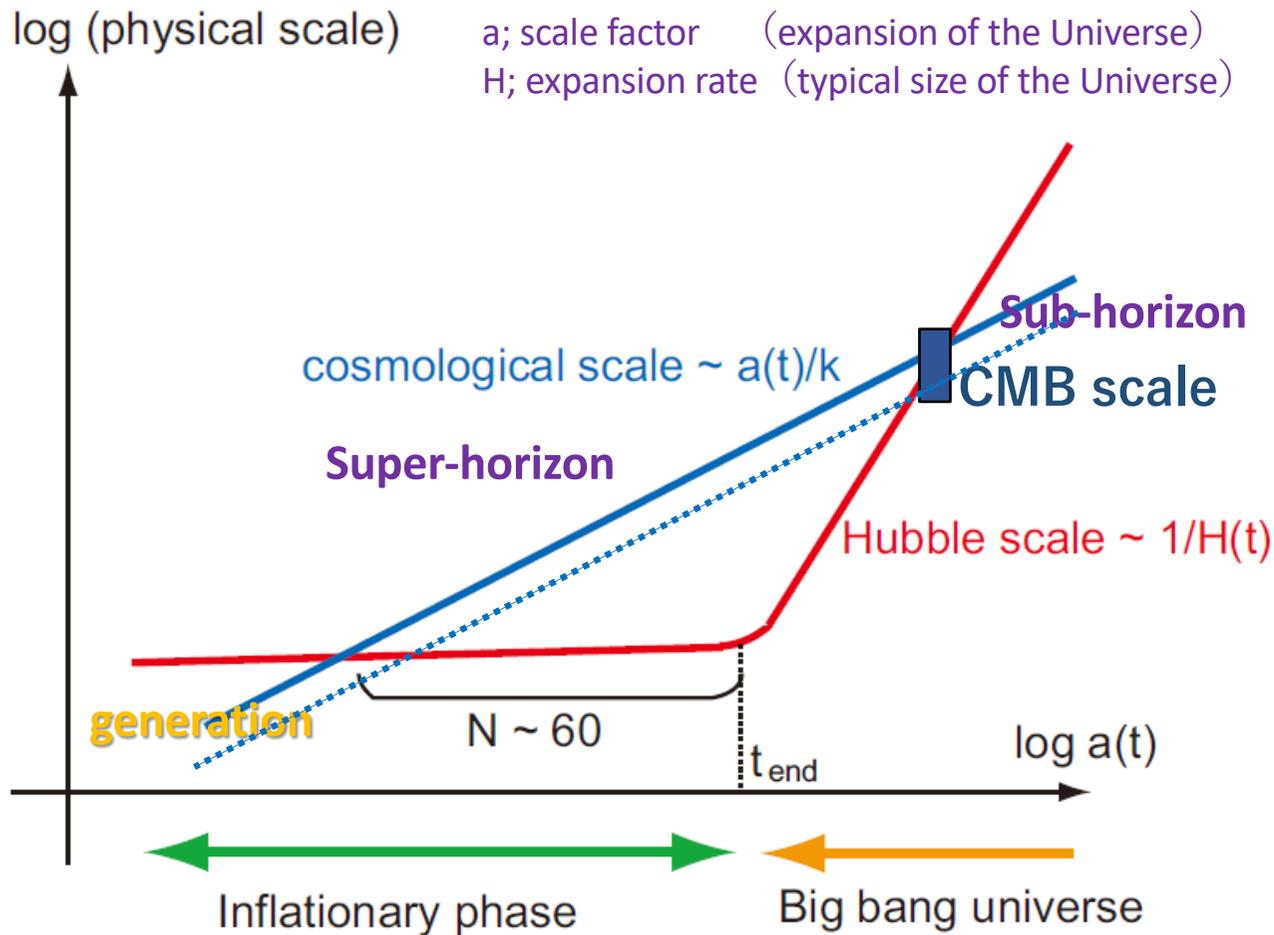
Single scalar inflation $\rightarrow f_{\text{NL}}^{\text{local}} \lesssim O(0.01)$

slow-roll suppression

How to discriminate?

- Higher order ?
- Smaller scales?

Primordial fluctuations from inflation



Quantum fluctuations (causal) are stretched by inflationary expansion



“classical” super-horizon (acausal) fluctuations (basically determined at the horizon exit)



primordial fluctuations with different scales (wavenumber) would bring us the information of different stages of inflation !!

Runnings of spectral index as a perturbative approach

Spectral index

$$\mathcal{P}_s(k) = A_s \left(\frac{k}{k_0} \right)^{n_s - 1 + \frac{1}{2}\alpha_s \ln(k/k_0) + \frac{1}{3!}\beta_s \ln^2(k/k_0) + \dots},$$

Taylor series of scale dependence of spectral index

For the slow-roll inflation, these parameters can be expressed w.r.t. slow-roll parameters as

$$\begin{aligned} n_s - 1 &= -6\epsilon + 2\eta, \\ \alpha_s &= -24\epsilon^2 + 16\epsilon\eta - 2\xi^{(2)}, \\ \beta_s &= -192\epsilon^3 + 192\epsilon^2\eta - 32\epsilon\eta^2 - 24\epsilon\xi^{(2)} + 2\eta\xi^{(2)} + 2\sigma^{(3)}, \end{aligned}$$

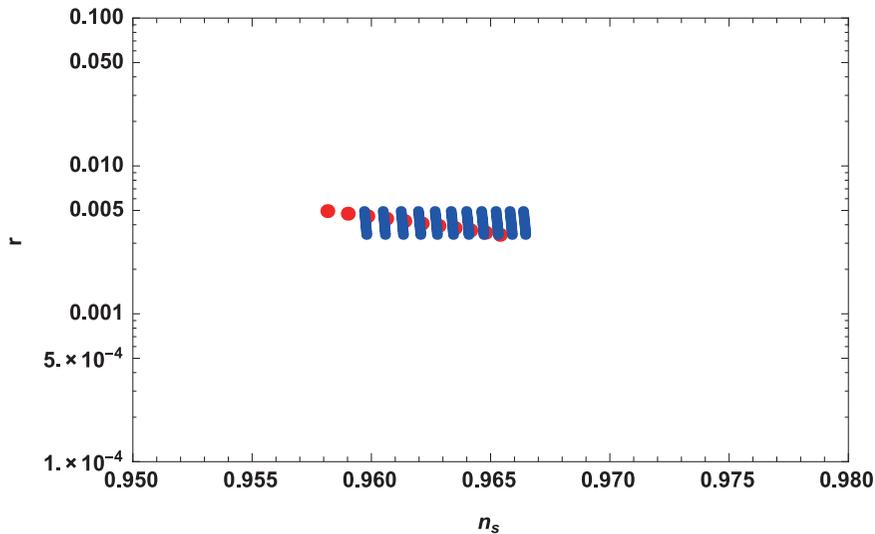
$$\xi^{(2)} \equiv M_{\text{pl}}^4 \frac{V'V'''}{V^2}, \quad \sigma^{(3)} \equiv M_{\text{pl}}^6 \frac{(\dot{V}')^2 V^{(4)}}{V^3},$$

V; inflaton's potential

depend on higher order slow-roll parameters which do not appear in “r” and “n_s”

As examples

$r - n_s$ plane

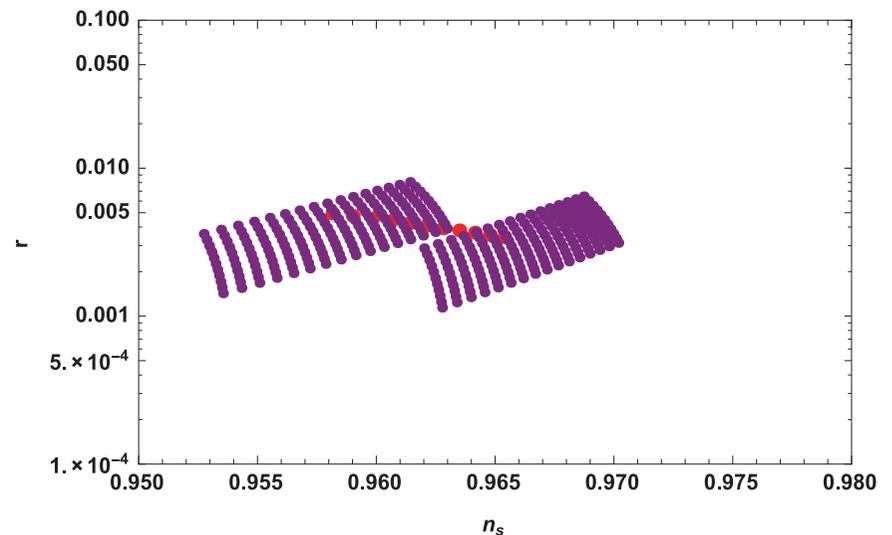


R^2 inflation ($N = 50 - 60$)

ϕ^4 -inflation with a massless spectator
($N = 50 - 60$)

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$$Q_\chi \equiv \frac{\mathcal{P}_s^{(\chi)}(k_0)}{\mathcal{P}_s^{(\phi)}(k_0) + \mathcal{P}_s^{(\chi)}(k_0)}$$



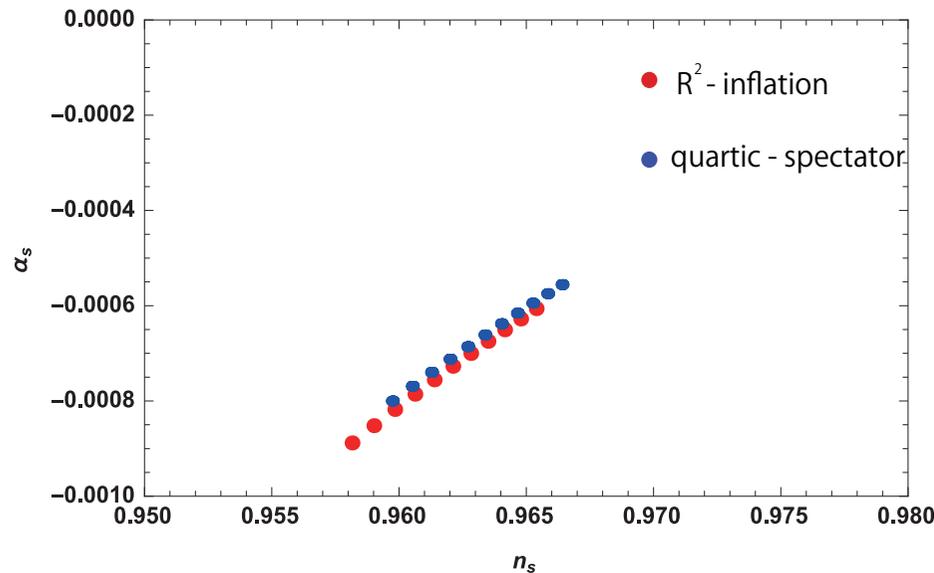
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$$V(\phi) = \Lambda^4 \left[1 - \cos \frac{\phi}{f} \right]$$

Sekiguchi, Takahashi, Tashiro, SY (2018)

As examples

$n_s - \alpha_s$ plane

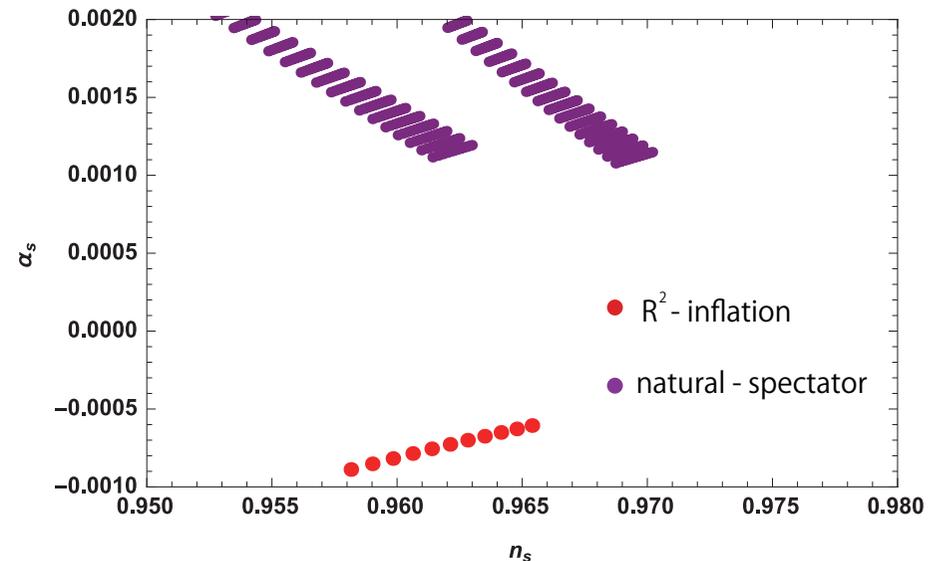


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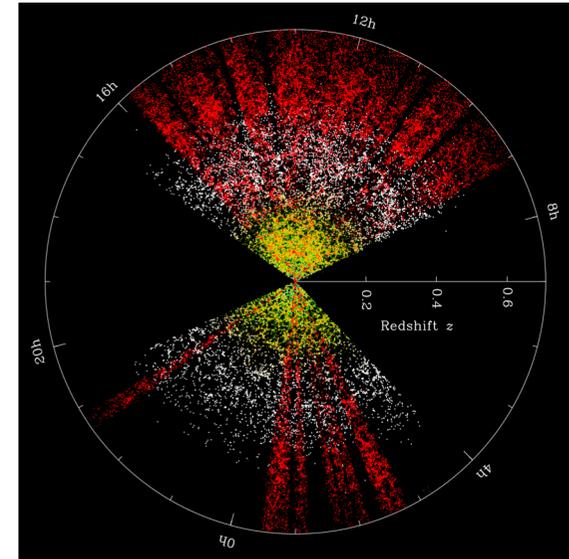
How to discriminate?

- Higher order ?
- Smaller scales?

SKA ??

Primordial NG in LSS

$$\zeta = \zeta_G + \frac{3}{5} f_{\text{NL}} (\zeta_G^2 - \langle \zeta_G^2 \rangle) + \dots$$



- higher order correlation functions (bispectrum, ...)

$$\langle \delta_L(\mathbf{k}_1) \delta_L(\mathbf{k}_2) \delta_L(\mathbf{k}_3) \rangle = (2\pi)^3 \delta(\mathbf{k}_1 + \mathbf{k}_2 + \mathbf{k}_3) B_L(k_1, k_2, k_3), \propto f_{\text{NL}}$$

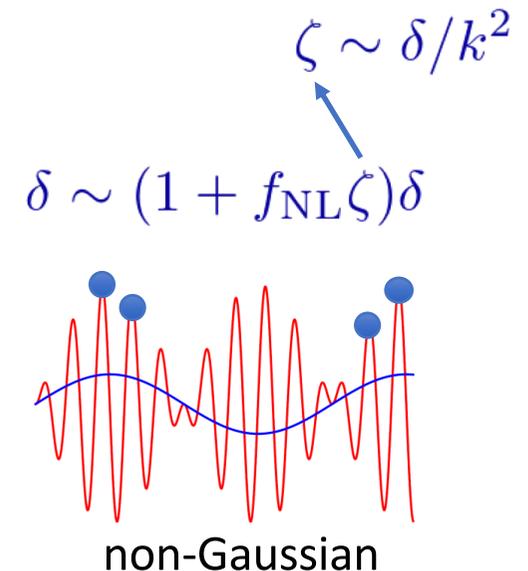
- Scale-dependent bias

$$P_{hh}(k) = (b_{eff}^E)^2 P_{mm}(k)$$

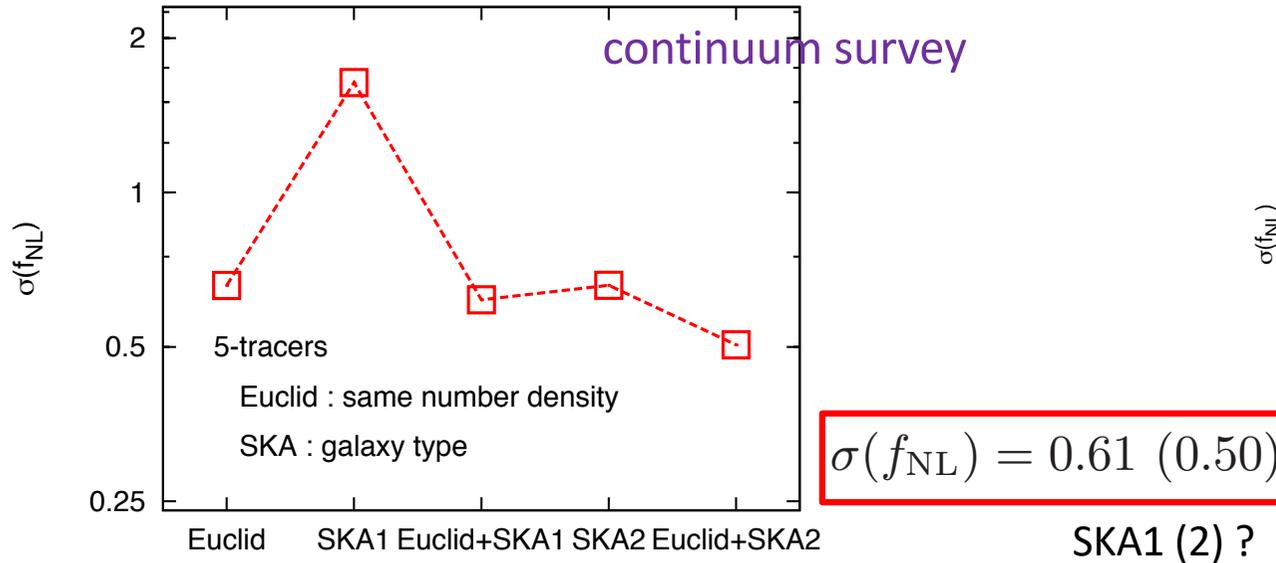
$$b_{eff}^E(k, z, f_{\text{NL}}) = b_G^E + 3f_{\text{NL}}(b_G^E - 1) \frac{H_0^2 \Omega_m \delta_c(z)}{c^2 T(k) k^2}$$

1/k² dependence !!

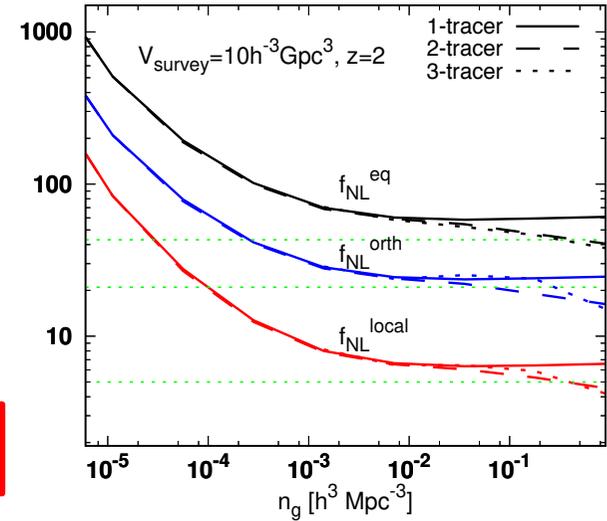
Galaxies, minihalos !!!



SKA as a galaxy survey



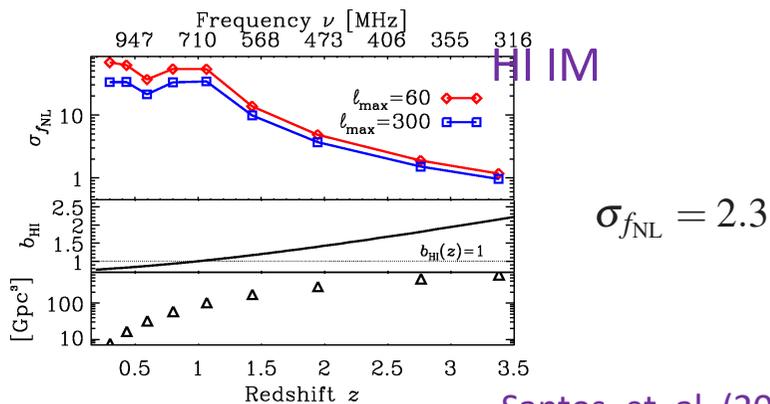
Yamauchi, Takahashi, Oguri (2014)



Yamauchi, SY, Takahashi (2016)

➔ Other types of NG ?

factor 2 improvement
compared with Planck



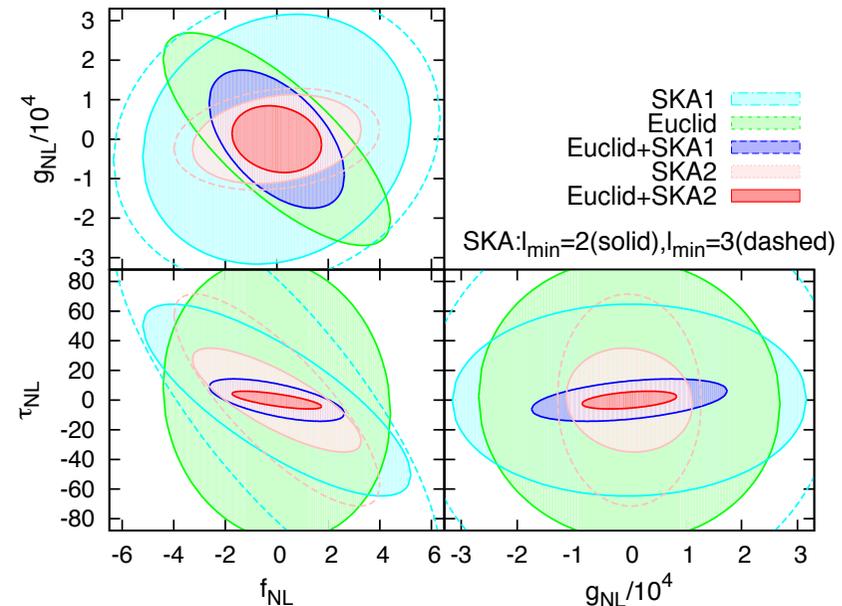
Santos, et. al. (2015)

SKA as a galaxy survey

Higher order non-Gaussianities?

f_{NL} ; a parameter related with
the primordial **bispectrum**
(3-pt. func.)

g_{NL} ; parameters related with
the primordial **trispectrum**
(4-pt. func.)



Yamauchi, Takahashi (2015)

SKA as a probe of EoR

Sekiguchi, Takahashi, Tashiro, SY (2018)

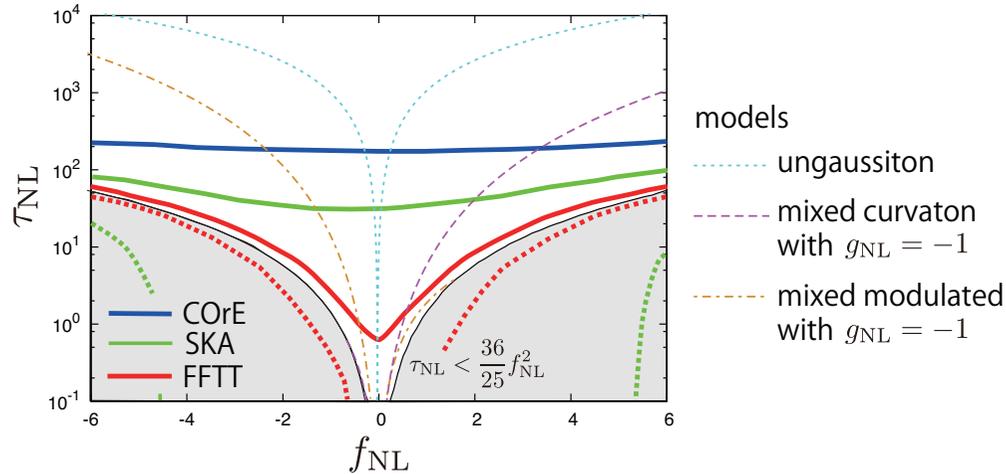
Minihalos as biased tracers

(lots of works, ...)

✓ virialized objects with the virial temperature $T < 10^4 \text{ K}$

too low to cause the star formation

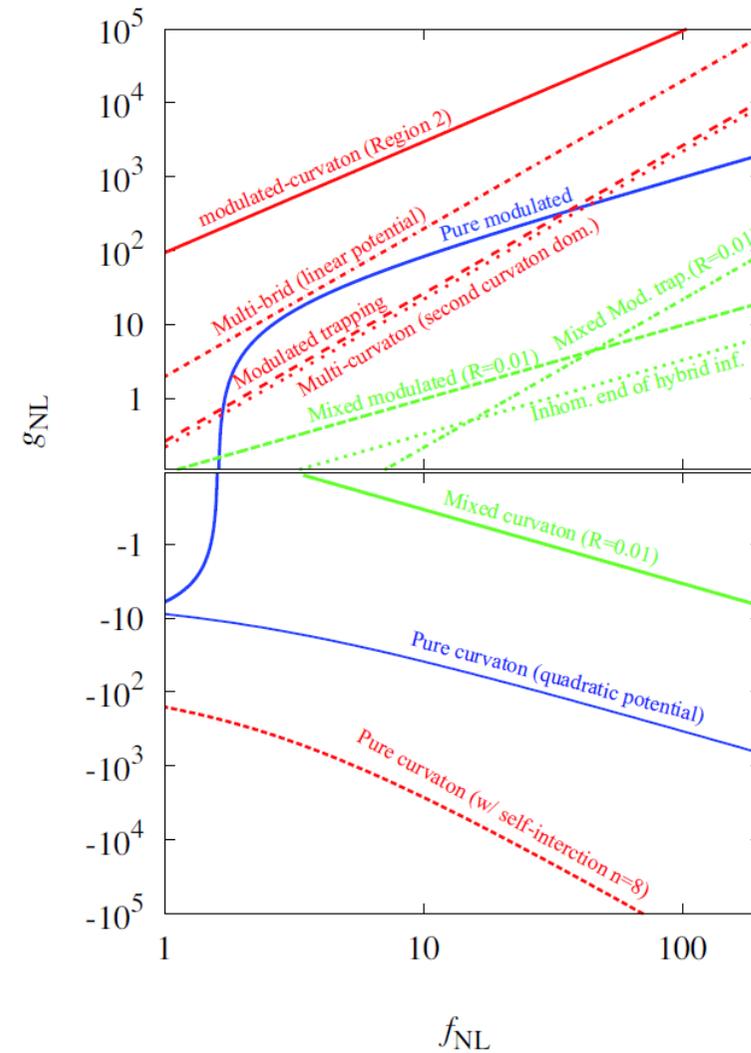
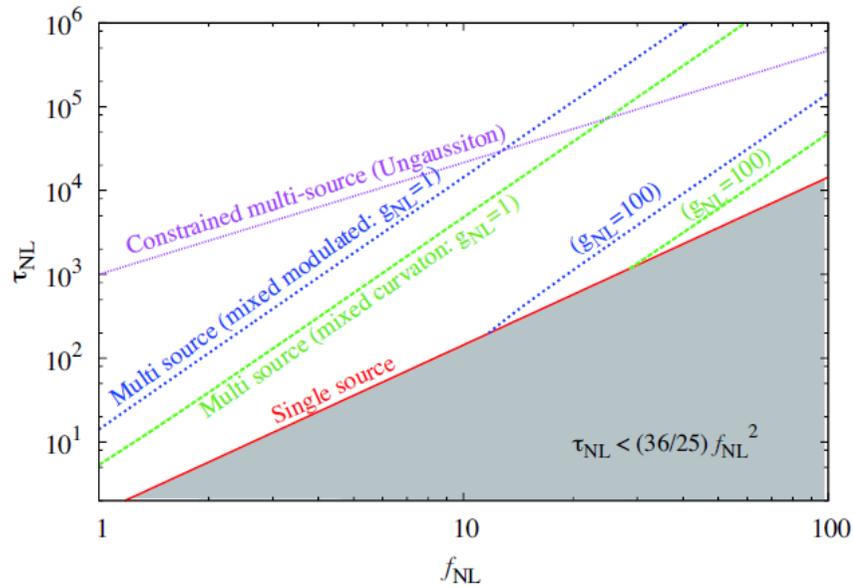
✓ filled neutral gas



dataset	Δf_{NL}	$\Delta g_{\text{NL}}/10^3$	$\Delta \tau_{\text{NL}}$
CMB alone			
Planck	4.0	41	610
COre	2.0	18	160
SKA	1.4	2.3	28
+Planck	1.3	2.3	28
+COre	1.1	2.2	27
FFTT	0.51	0.79	0.59
+Planck	0.50	0.78	0.58
+COre	0.48	0.75	0.58

Powerful to discriminate large NG models (multi-inflation) !!!

Higher NGs in multi-scalar inf.



SKA as a probe of EoR

Sekiguchi, Takahashi, Tashiro, SY (2018)

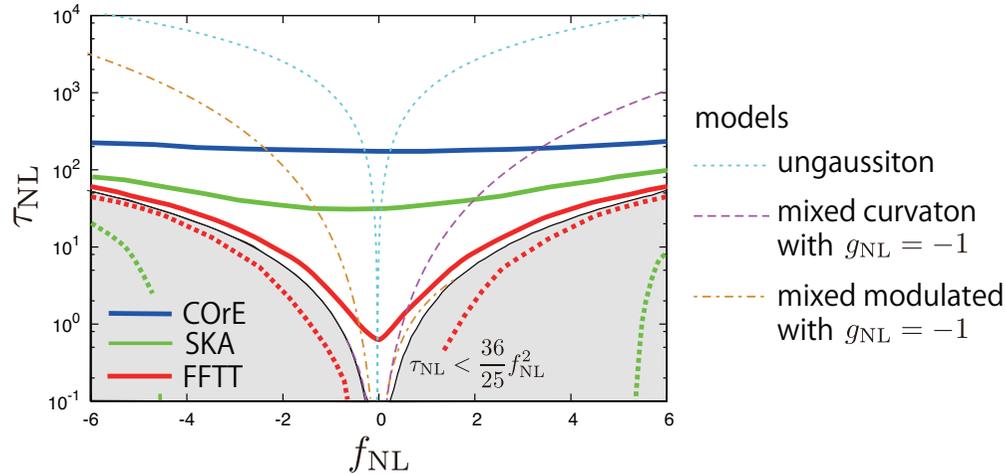
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How to discriminate?

- Higher order ?
- Smaller scales?

SKA ??

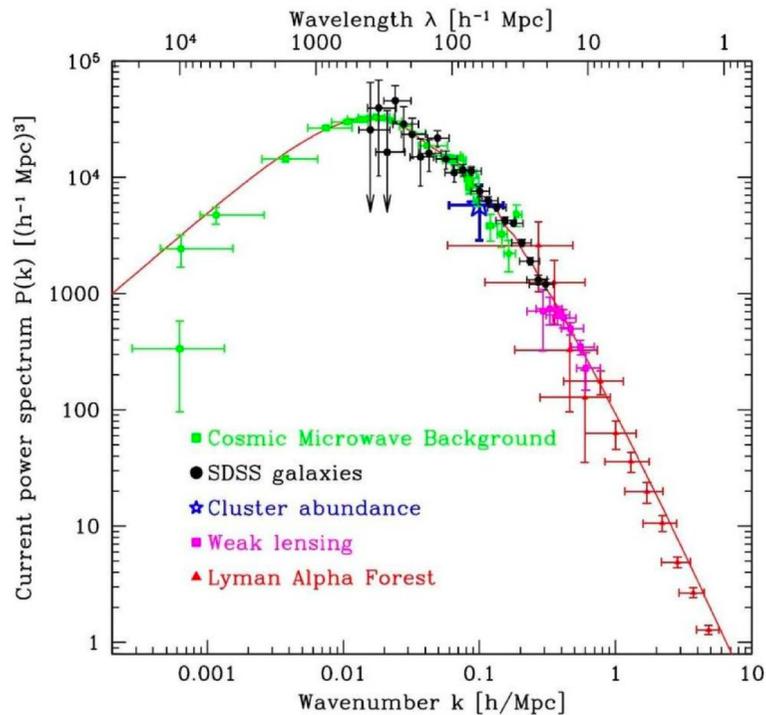
SKA as a probe of EoR

Matter fluctuations in EoR

Kohri, et al. (2013)

(lots of works, ...)

➤ High-z → “gravitational” non-linearity is not so large (~1 Mpc?)



	δn_s	$\delta \alpha_s$	$\delta \beta_s$
Planck	4.11×10^{-3}	6.59×10^{-3}	9.95×10^{-3}
Planck + SKA phase1	2.03×10^{-3}	2.90×10^{-3}	2.21×10^{-3}
Planck + SKA phase2	1.73×10^{-3}	2.36×10^{-3}	1.52×10^{-3}
Planck + Omniscope	6.04×10^{-4}	1.07×10^{-3}	7.31×10^{-4}
CMBpol	2.10×10^{-3}	2.36×10^{-3}	4.37×10^{-3}
CMBpol + SKA phase1	1.46×10^{-3}	2.07×10^{-3}	1.61×10^{-3}
CMBpol + SKA phase2	1.33×10^{-3}	1.84×10^{-3}	1.21×10^{-3}
CMBpol + Omniscope	5.53×10^{-4}	1.00×10^{-3}	6.86×10^{-4}
COrE	2.13×10^{-3}	2.43×10^{-3}	4.47×10^{-3}
COrE + SKA phase1	1.47×10^{-3}	2.09×10^{-3}	1.63×10^{-3}
COrE + SKA phase2	1.34×10^{-3}	1.85×10^{-3}	1.22×10^{-3}
COrE + Omniscope	5.54×10^{-4}	1.00×10^{-3}	6.87×10^{-4}

Tegmark et al. (2004)

SKA as a probe of EoR

Sekiguchi, Takahashi, Tashiro, SY (2017)
 Shimabukuro, Ichiki, Inoue, SY (2014), ...

Minihalos as a probe of smaller scales

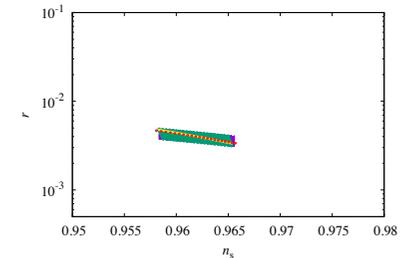
- ✓ virialized objects with the virial temperature $T < 10^4 \text{ K}$

Iliev et al. (2002), ...

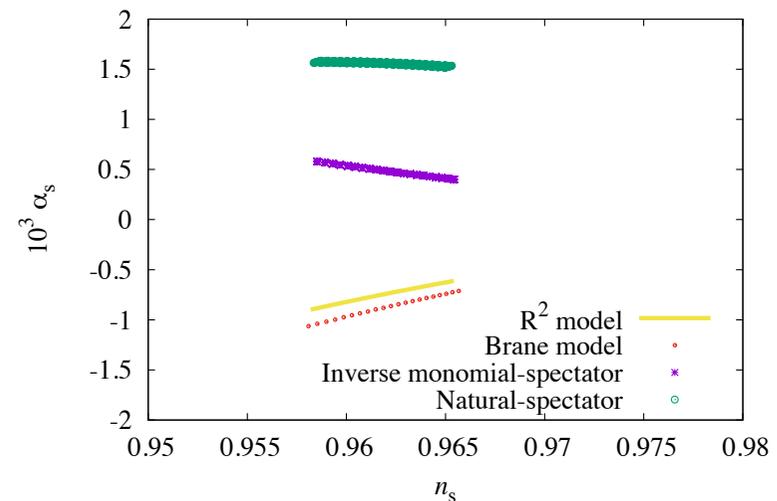
too low to cause the star formation

- ✓ filled neutral gas

- ✓ corresponding scales; $20 \text{ Mpc}^{-1} < k < 500 \text{ Mpc}^{-1}$



	$10^{-3} \Delta n_s$	$10^{-3} \Delta \alpha_s$	$10^{-3} \Delta \beta_s$
Planck	7.7	10.7	15.1
COrE	3.2	2.9	6.5
SKA	4.6	2.9	1.5
FFTT	2.4	1.6	0.79
Planck+SKA	1.7	2.0	0.63
Planck+FFTT	1.3	1.3	0.44
COrE+SKA	1.2	1.6	0.39
COrE+FFTT	0.95	1.1	0.28



We can distinguish !

Observational inflation cosmology

SKA

- Higher order

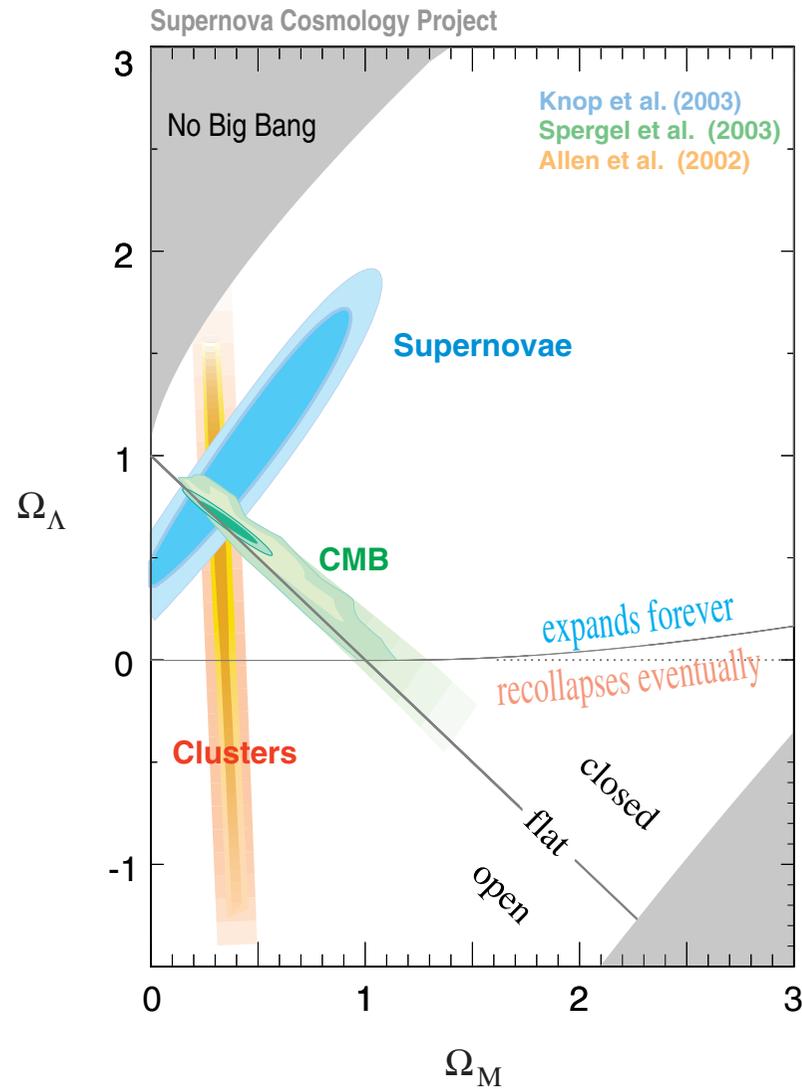
$$\sigma(f_{\text{NL}}) = 0.61 \text{ (0.50)}$$

- Smaller scales

	$10^{-3}\Delta n_s$	$10^{-3}\Delta\alpha_s$	$10^{-3}\Delta\beta_s$
Planck	7.7	10.7	15.1
COrE	3.2	2.9	6.5
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Dark energy

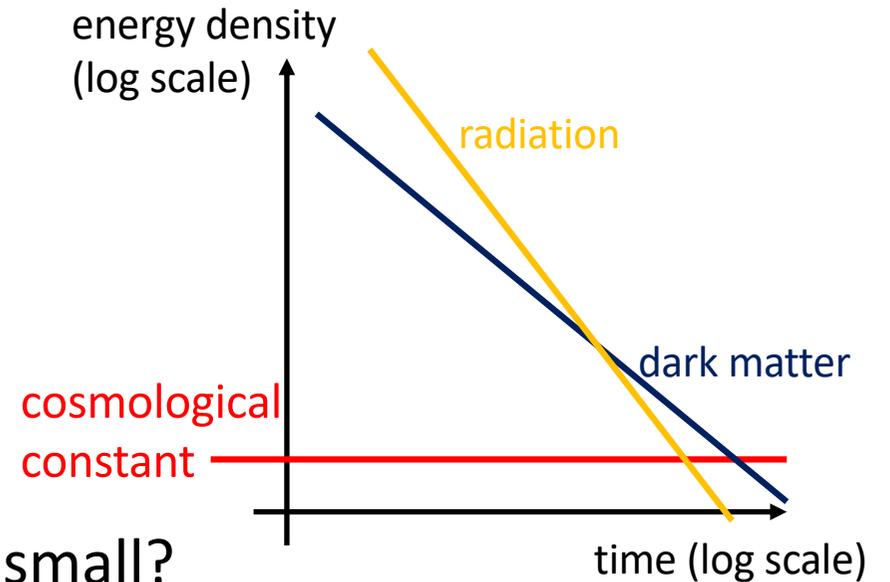
Accelerated expansion of the Universe at present ...



Most probable?

- Cosmological constant

→ should be resolved: why so small?
why now?



$$\rho_{\Lambda} \ll M_{\text{Pl}}^4$$

resolved by string landscape picture?

Susskind, Weinberg, ...

not allowed by swampland conjecture ??

Obied, Ooguri, Spodyneiko, Vafa (2018)

cosmological constant; $w = -1$



Inflation like

- Quintessence (potential driven)

Lots of models ...

(like an inflation zoo ...)

equation of state parameter is

$$w = \frac{\frac{1}{2}\dot{\phi}^2 - V}{\frac{1}{2}\dot{\phi}^2 + V} > -1$$

c.f. cosmological constant; $w = -1$

k-essence $w = \frac{2XP_X - P}{P}$

would be smaller than -1 .. (violation of energy condition?)

Thawing and freezing

- Quintessence (potential driven)

Lots of models ...

motivated by SUGRA, ...

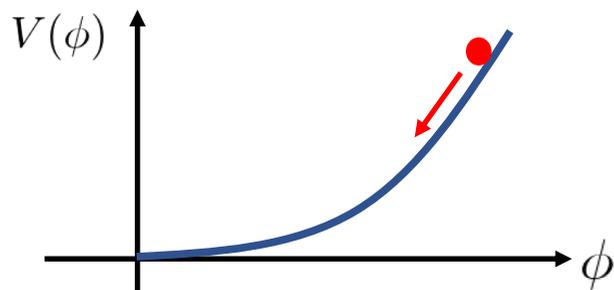
(like an inflation zoo ...)

Basically, two types of quintessence model

See, e.g., Caldwell and Linder (2005), ...

Thawing model

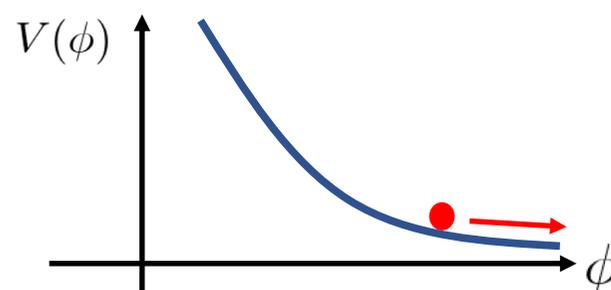
e.g., $V \propto \phi^n$ ($n > 0$)



starts slow-rolling (thawing)
around the present time

Freezing model (tracker)

e.g., $V \propto \phi^{-n}$ ($n > 0$)



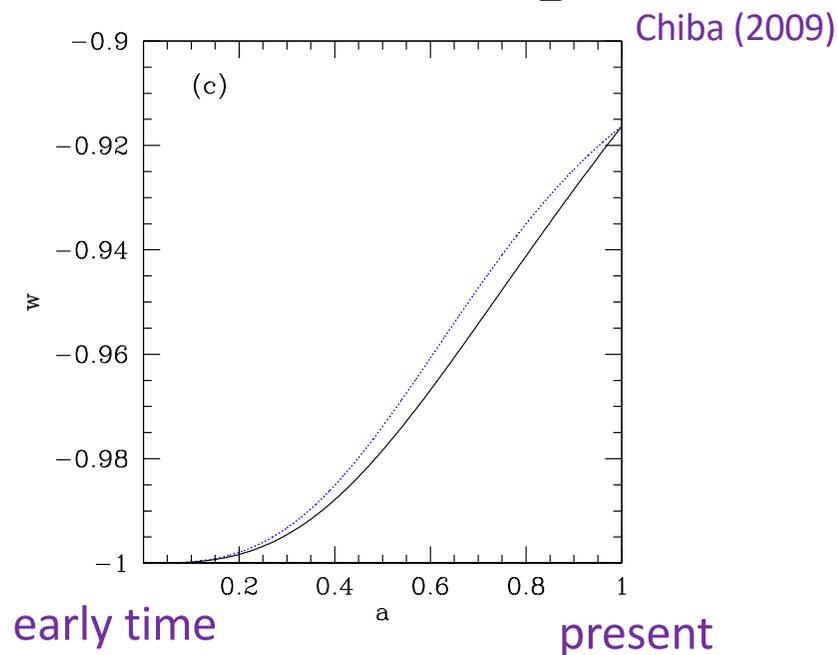
fast rolling \rightarrow slow rolling (freezing)

Thawing and freezing

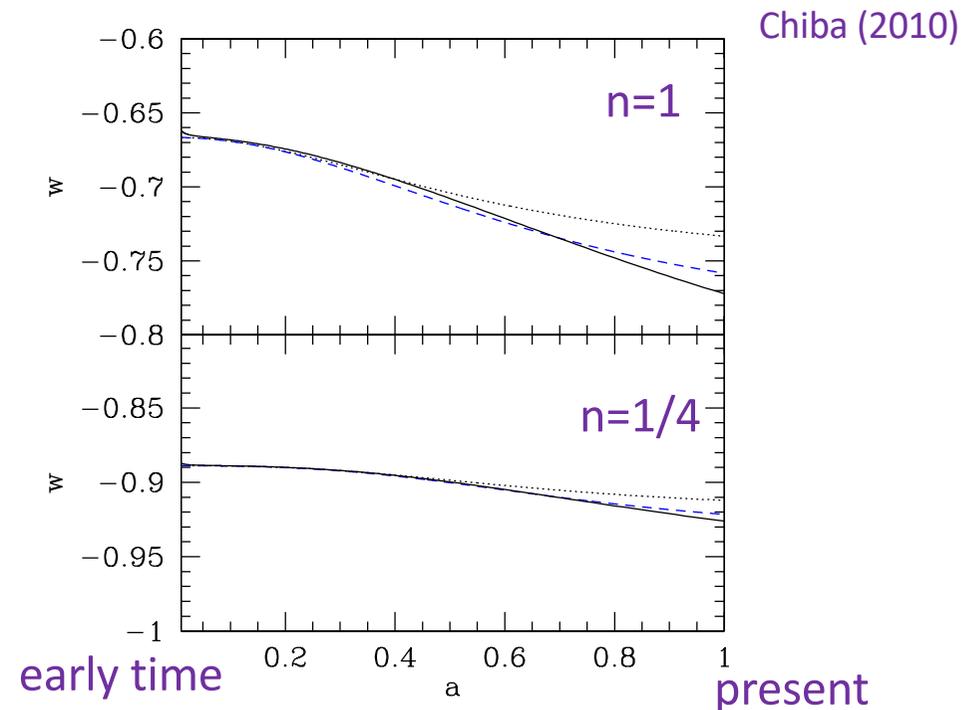
- Quintessence (potential driven)

Evolution of equation of state

Thawing model $V = \frac{1}{2}m^2\phi^2$



Freezing model $V \propto \phi^{-n} (n > 0)$



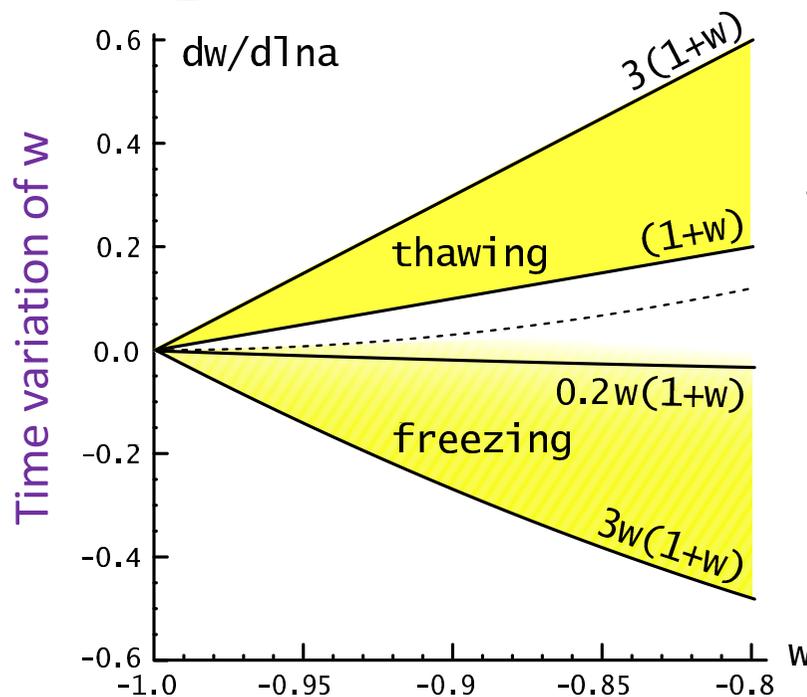
Thawing and freezing

- Quintessence (potential driven)

Evolution of equation of state

Thawing model $V = \frac{1}{2}m^2\phi^2$

Freezing model $V \propto \phi^{-n} (n > 0)$



To discriminate these models,
It should be important to observe
**not only equation of state but also
its time dependence !**

Modified gravity

- Scalar tensor theory

→ non-minimally coupled scalar field $\supset \phi R$

could also include the derivative coupling $\supset G_{\mu\nu} \partial^\mu \phi \partial^\nu \phi$

In general, we can consider the Lagrangian
which has infinite terms with including higher order derivatives ...

Infinite possible theories ?

Is there any guiding principles?

- from the first principle (string theory, or ...?) (top-down)
- Based on some philosophy (respect some symmetry, stability condition, ...)

→ free from ghost instabilities !!

Modified gravity

see, e.g., Kobayashi, 1901.07183 (review paper)

- **Horndeski theory**

Lagrangian;

$$\mathcal{L} = G_2(\phi, X) - G_3(\phi, X)\square\phi + G_4(\phi, X)R + G_{4X} [(\square\phi)^2 - \phi^{\mu\nu}\phi_{\mu\nu}] \\ + G_5(\phi, X)G^{\mu\nu}\phi_{\mu\nu} - \frac{G_{5X}}{6} [(\square\phi)^3 - 3\square\phi\phi^{\mu\nu}\phi_{\mu\nu} + 2\phi_{\mu\nu}\phi^{\nu\lambda}\phi_{\lambda}^{\mu}],$$

G_i ($i = 2, 3, 4, 5$) are arbitrary functions of ϕ and X

$$f_X := \partial f / \partial X$$

$$X := -g^{\mu\nu}\phi_{\mu}\phi_{\nu}/2$$

$$\phi_{\mu} := \nabla_{\mu}\phi,$$

The most general scalar-tensor theory
having second-order field equations in 4D

free from ghost instabilities associated with the higher derivative terms

could have extra d.o.f.

Modified gravity

see, e.g., Kobayashi, 1901.07183 (review paper)

- **Horndeski theory**

Lagrangian;

$$\mathcal{L} = G_2(\phi, X) - G_3(\phi, X)\square\phi + G_4(\phi, X)R + G_{4X} [(\square\phi)^2 - \phi^{\mu\nu}\phi_{\mu\nu}] \\ + G_5(\phi, X)G^{\mu\nu}\phi_{\mu\nu} - \frac{G_{5X}}{6} [(\square\phi)^3 - 3\square\phi\phi^{\mu\nu}\phi_{\mu\nu} + 2\phi_{\mu\nu}\phi^{\nu\lambda}\phi_{\lambda}^{\mu}],$$

Due to the existence of **non-minimal coupling between scalar d. o. f. and gravity**,

in this theory, the gravitational law would be changed!

That is, we can test not only by cosmological observations but also by local gravity test, GW experiments, and more..

Modified gravity

see, e.g., Kobayashi, 1901.07183 (review paper)

- **Beyond ?**

Horndeski theory: The most general scalar-tensor theory
having second-order field equations in 4D

little bit strong?



Degenerate Higher-Order Scalar-Tensor theories (DHOST theories)

see, e.g., Langlois, 1811.06271 (review paper)

$$\mathcal{L} = f(\phi, X)R + \sum_{I=1}^5 A_I(\phi, X)L_I, \quad \begin{aligned} L_1 &= \phi_{\mu\nu}\phi^{\mu\nu}, & L_2 &= (\square\phi)^2, & L_3 &= \square\phi\phi^\mu\phi^\nu\phi_{\mu\nu} \\ L_4 &= \phi^\mu\phi_{\mu\alpha}\phi^{\alpha\nu}\phi_\nu, & L_5 &= (\phi^\mu\phi^\nu\phi_{\mu\nu})^2. \end{aligned}$$

With so-called “degeneracy conditions”, pathological extra d. o. f. doesn’t appear.

What is DE?

- Points for observations

- ✓ Cosmological constant $w = -1$

- ✓ Quintessence models – thawing type $dw/dt > 0$

- $w > -1$ -- freezing type $dw/dt < 0$

- ✓ Scalar-tensor theories – Horndeski, DHOST theories,...

measurement the gravitational law

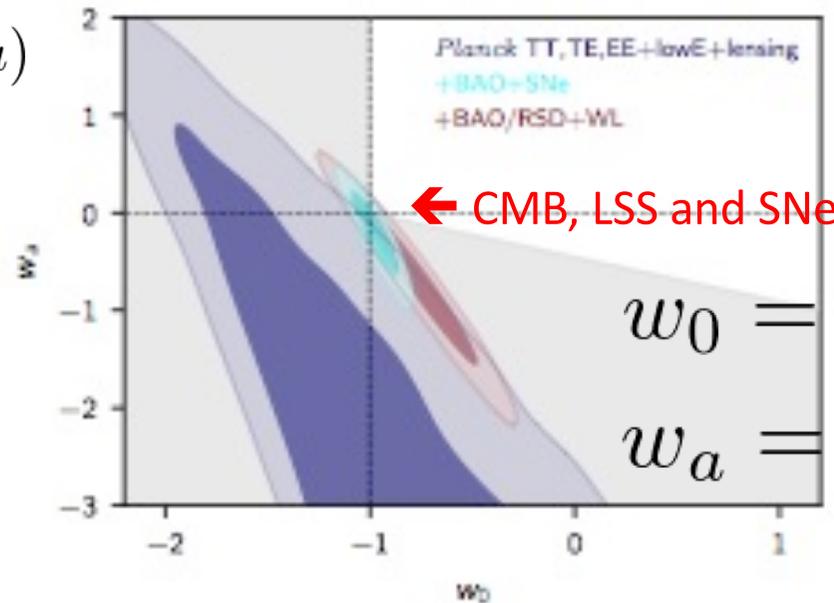
Equation of state

- Expansion of the Universe

In principle,
if we could measure the long time history of the expansion rate of the Universe,
we can also get the information about the evolution of the “equation of state”.

$$w = w_0 + w_a(1 - a)$$

Perturbative
parameterization



$$w_0 = -0.961 \pm 0.077$$

$$w_a = -0.28^{+0.31}_{-0.27}$$

Planck (2018)

Cosmological gravitational law

- Evolution of matter inhomogeneities in the Universe

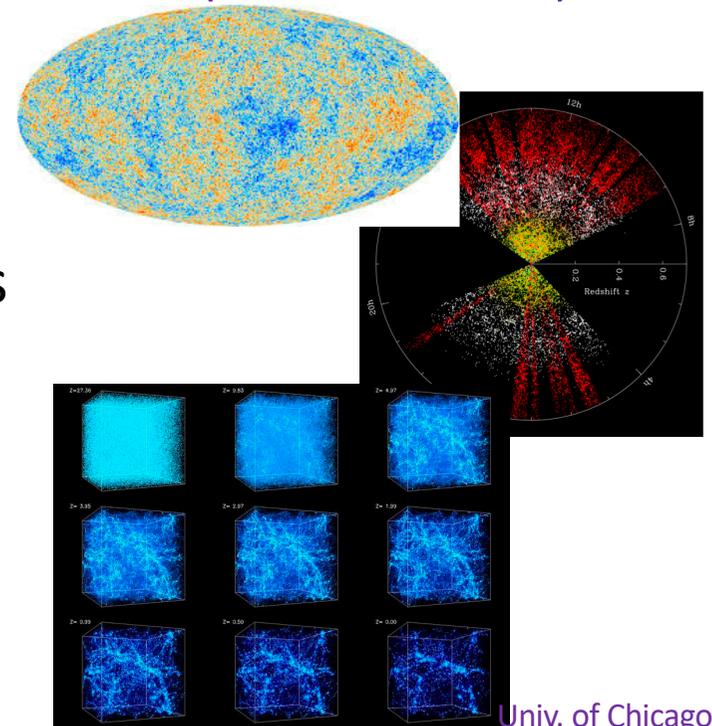
In cosmology, we treat the spatial inhomogeneities of matter distributions, (including galaxy distributions on large scales), as perturbations on the background homogeneous and isotropic Universe (FLRW Universe).

$$\rho(t, \mathbf{x}) = \bar{\rho}_m(t) (1 + \delta(t, \mathbf{x}))$$

Such a matter inhomogeneity evolves through the gravitational interaction!



valuable information about the "cosmological" gravitational law!!



Linear growth

see, e.g., Kobayashi, 1901.07183 (review paper)

- Evolution of matter inhomogeneities in the Universe

Measure

the “linear” growth of matter (DM) density contrast (inhomogeneities),

to find the cosmological gravitational law

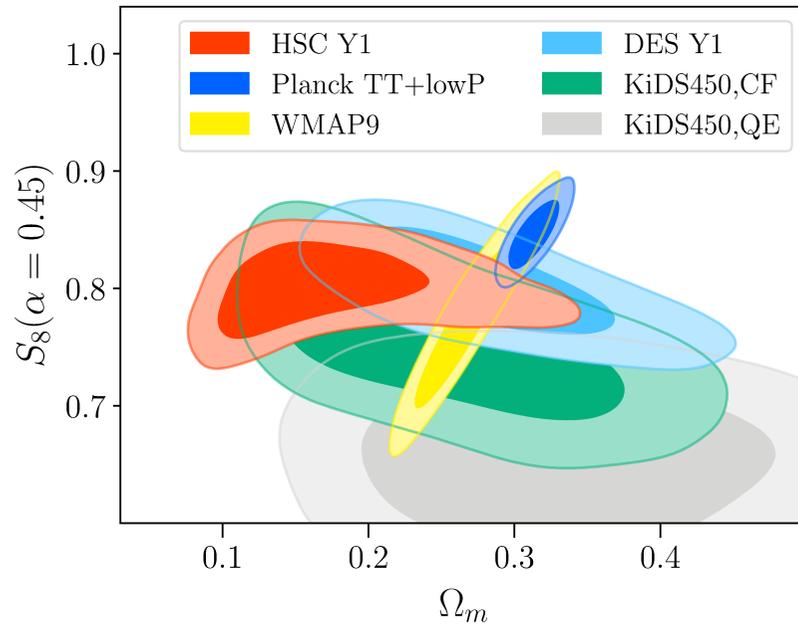
and test the scalar-tensor theories !

usually, parameterized as

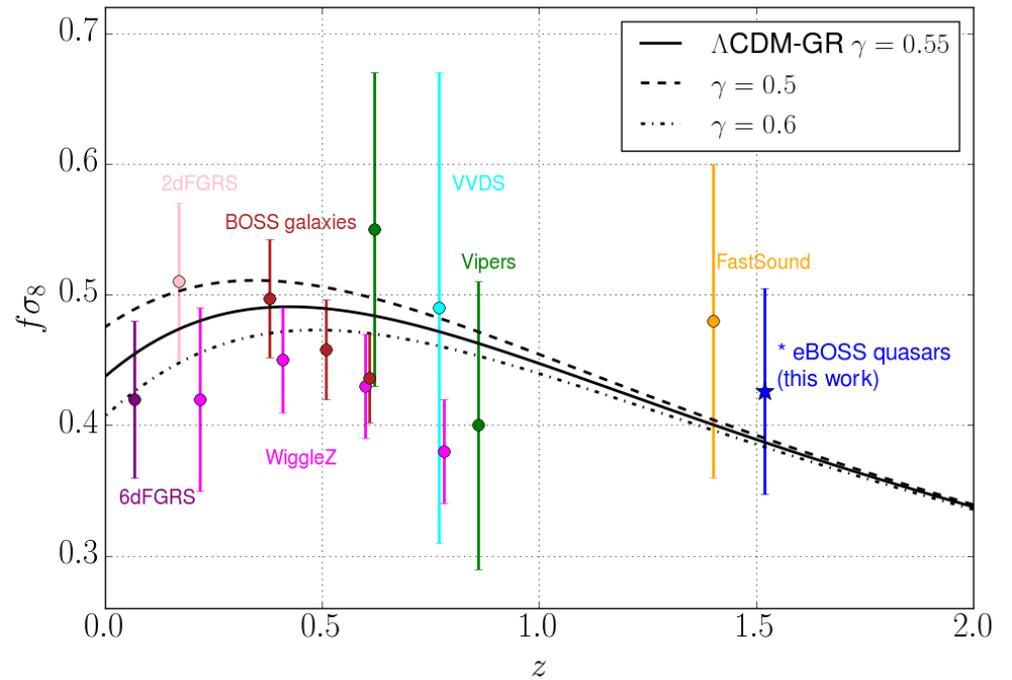
$$f := \frac{d \ln \delta(t)}{d \ln a} \quad \text{or} \quad f = \Omega_m^\gamma \quad \text{In GR, } \gamma = 0.55$$

a is a scale factor (time coordinate)

Linear growth



arXiv:1809.09148v2



Zarrouk et al. (2018)

What is DE?

- Points for observations

- ✓ Cosmological constant $w = -1$

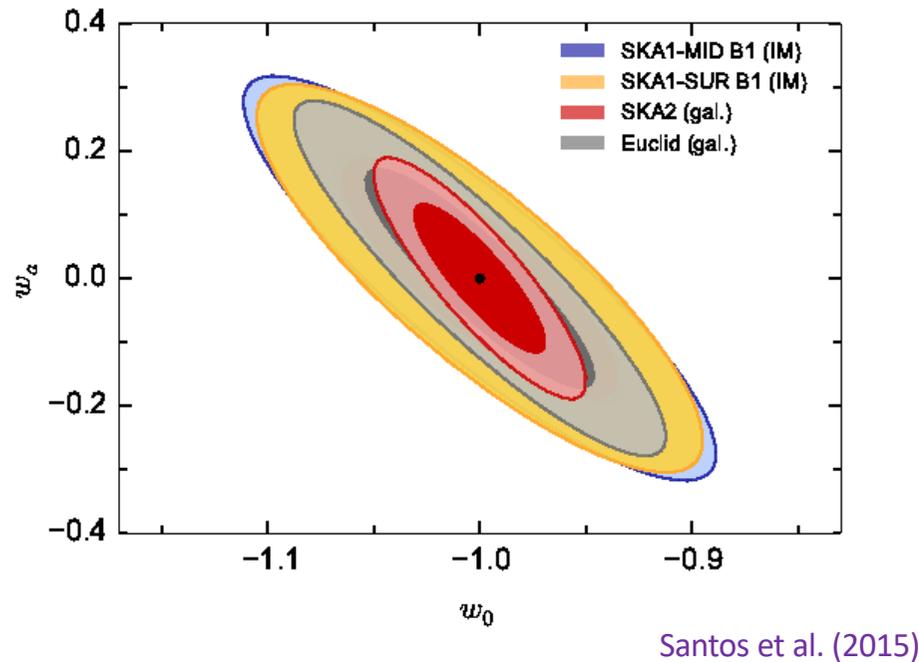
- ✓ Quintessence **SKA ??** :type $dw/dt > 0$

- $w > -\frac{1}{3}$ -- freezing type $dw/dt < 0$

- ✓ Scalar-tensor theories – Horndeski, DHOST theories,...

measurement the gravitational law

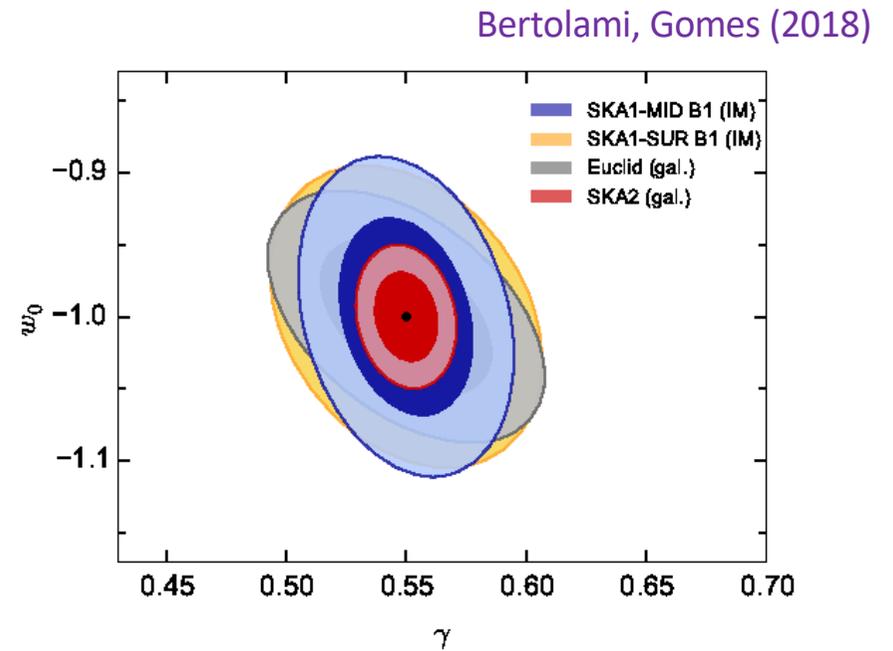
SKA as a galaxy survey / HI intensity mapping



Planck (2018)

$$w_0 = -0.961 \pm 0.077$$

$$w_a = -0.28^{+0.31}_{-0.27}$$

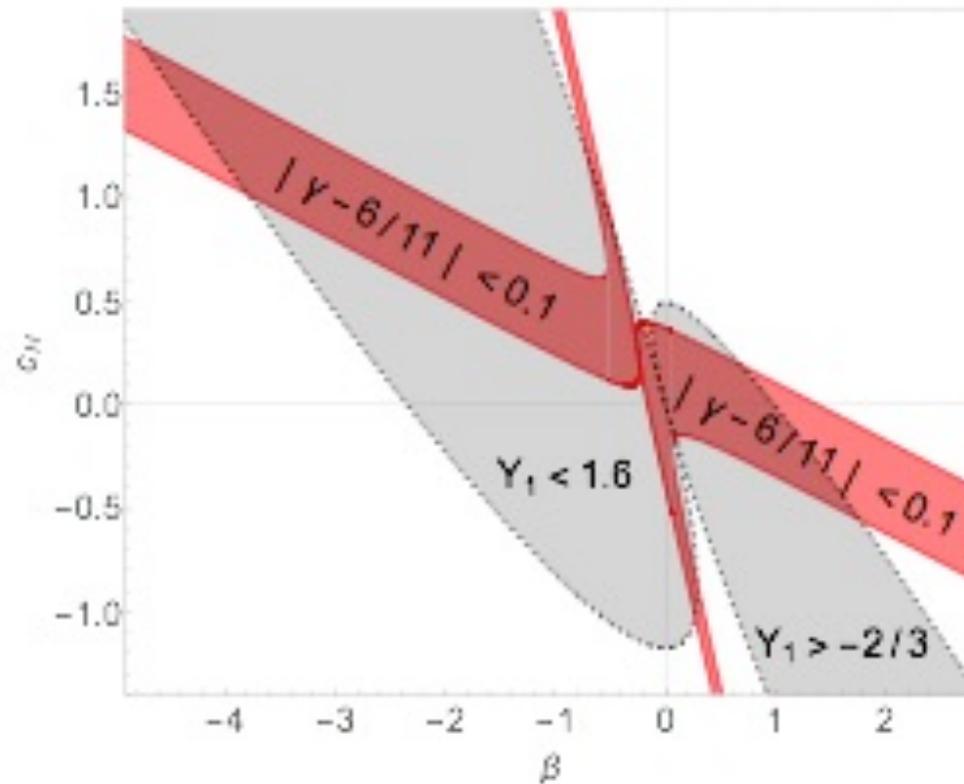


BOSS DR14 (2018)

$$\gamma = 0.55 \pm 0.19$$

Implication for ST theories

Hirano, Kobayashi, Yamauchi, SY (2019)



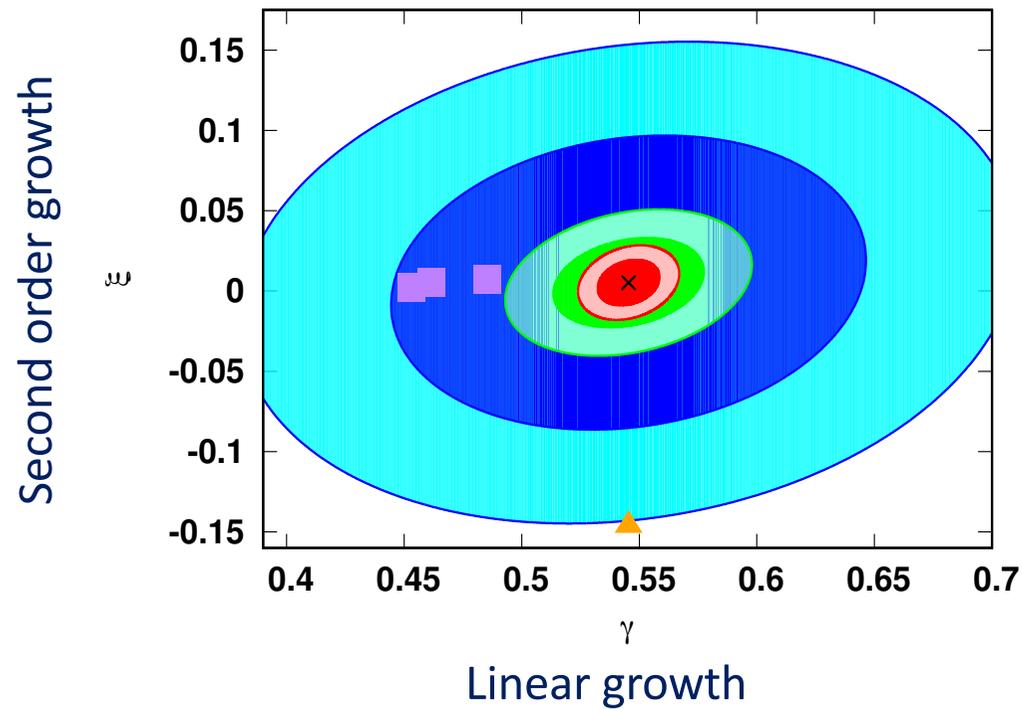
Modification of gravity
in astrophysical bodies;

$$\frac{d\Phi}{dr} = \frac{G_N M(r)}{r^2} + \frac{\Upsilon_1 G_N}{4} \frac{d^2 M(r)}{dr^2}$$

Growth in higher order ?

Yamauchi, Tashiro, SY (2017)

expected constraint from galaxy bispectrum



assuming · SKA1MID(blue), SKA2(red) and Euclid(green)

What is DE?

SKA ??

- Points for observations

- ✓ Cosmological constant

$$\Delta w < 0.05$$

- ✓ Quintessence models – thawing type

$$\Delta(dw/dt) < 0.1$$

- freezing type

- ✓ Scalar-tensor theories – Horndeski, DHOST theories,...

$$\Delta \gamma < 0.02$$

Dark matter

Dark matter

- Existence of dark matter

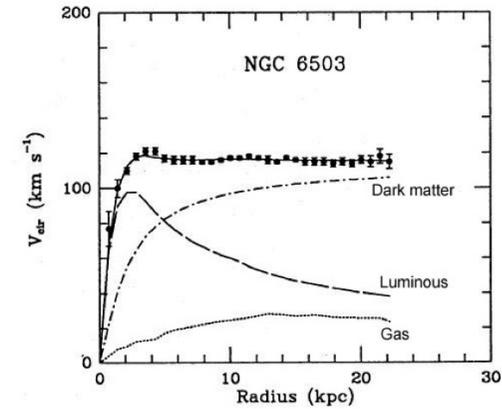
- ✓ Lots of astro/cosmological observations (rotation curve, LSS, CMB)

Basically, gravitational interaction

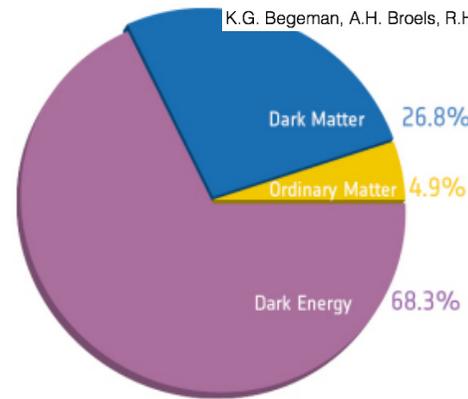


Unknown "weakly" interacting particles?

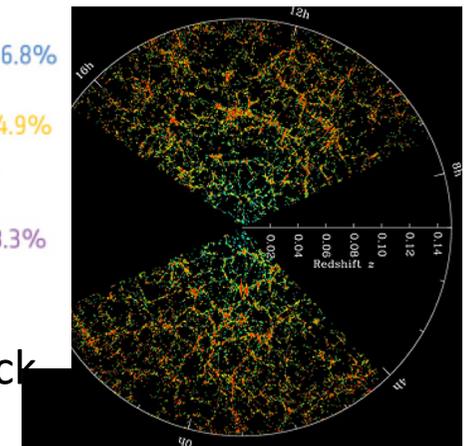
SUSY particles (WIMP LSP),
QCD axion, sterile neutrino,
Axion Like Particles (string theory) ...



K.G. Begeman, A.H. Broels, R.H. Sanders. 1991. Mon.Not.RAS 249, 523.



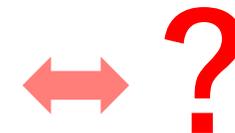
©Planck



from SDSS

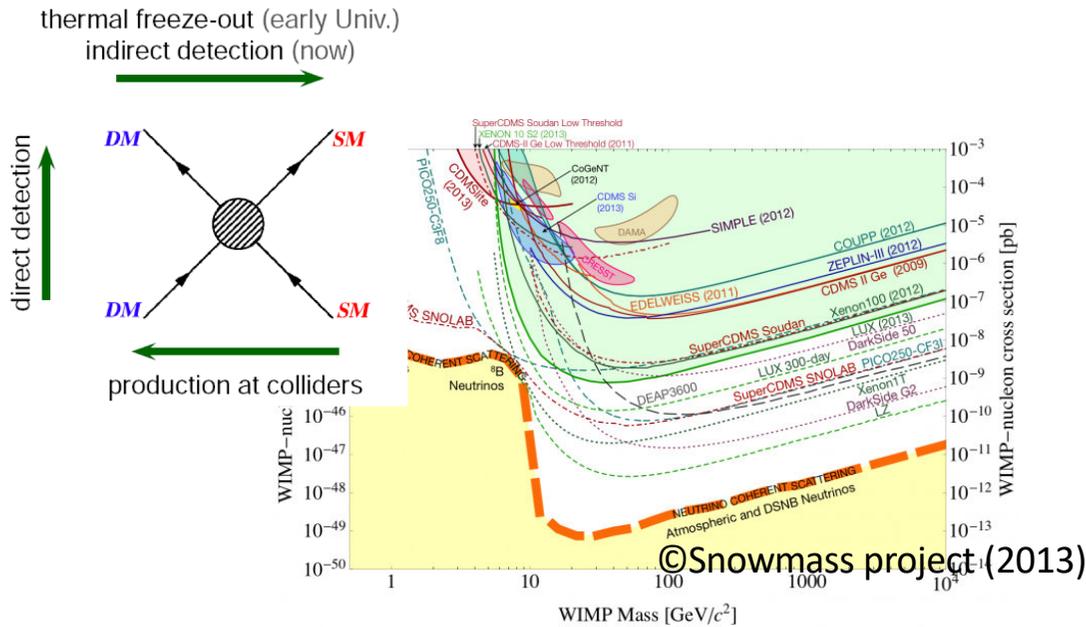
Standard Model of Elementary Particles

	three generations of matter (fermions)			interactions / force carriers (bosons)	
	I	II	III		
mass	=2.2 MeV/c ²	=1.28 GeV/c ²	=173.1 GeV/c ²	0	=125.09 GeV/c ²
charge	2/3	2/3	2/3	0	0
spin	1/2	1/2	1/2	1	0
QUARKS	u up	c charm	t top	g gluon	H higgs
	d down	s strange	b bottom	γ photon	
	e electron	μ muon	τ tau	Z Z boson	
LEPTONS	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	W W boson	
				SCALAR BOSONS	
				GAUGE BOSONS vector bosons	



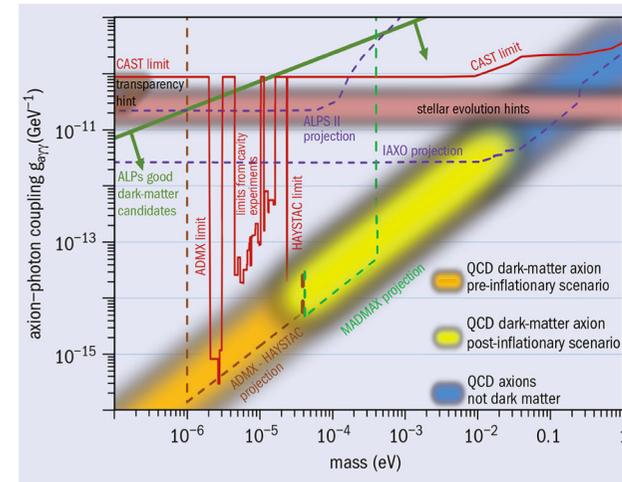
unknown particles?

- lots of particle experiments

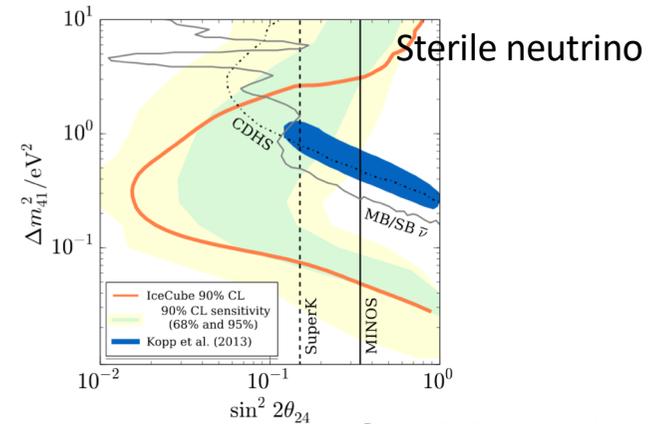


- ➔ No evidence ...
- ➔ Beyond standard "WIMP"?

axion - photon coupling



©Majorovits (MADMAX)



©IceCube collabo.

BHs as DM

- How about other candidates?

Basically, only gravitational interaction → **Black holes ? ?**

However,

The diagram shows a timeline of the universe's evolution from the Big Bang to the present. Key stages include: Big Bang, Cosmic inflation (Origin of fluctuations), Particles form (Ordinary matter particles are coupled to dark matter particles start building structures), Recombination (Ordinary matter particles decouple from the Cosmic Microwave Background is released), Dark ages (Ordinary matter particles fall into structures created by dark matter), First stars & galaxies, Galaxy evolution (Clusters of galaxies and superclusters form), Today, Clusters of galaxies, Galaxy, and Solar System. A white text box is overlaid on the timeline, containing the text: 'It is completely difficult to explain the dark matter by standard astrophysical black holes (stellar BHs) ...' Below this, another white text box contains the text: 'How about if BH could be formed in the early Universe? → Primordial black hole!!'

Success of standard big bang model

It is completely difficult to explain the dark matter by standard astrophysical black holes (stellar BHs) ...

**How about if BH could be formed in the early Universe?
→ Primordial black hole!!**

Basics of PBH

Zeldovich and Novikov (1967)

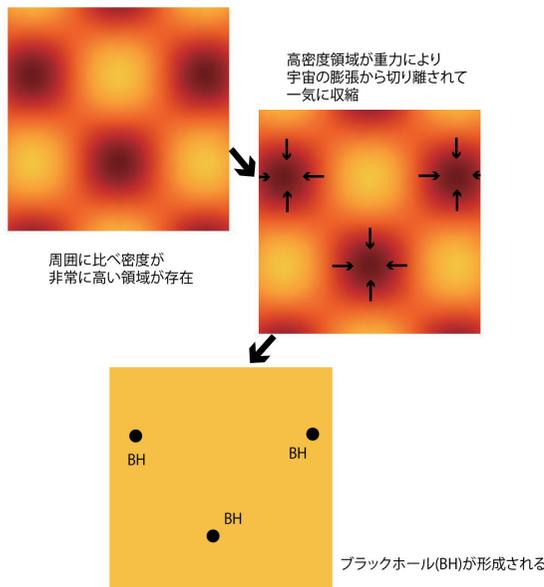
Hawking (1971)

Carr and Hawking (1974), ...

- Primordial Black Hole (PBH)

- ✓ BHs formed in the early Universe (after inflation)
- ✓ direct gravitational collapse of a **overdense region (horizon scale)**
- ✓ mass of formed BH ~ Hubble horizon mass at the formation

especially for the PBH formed in the radiation-dominated era

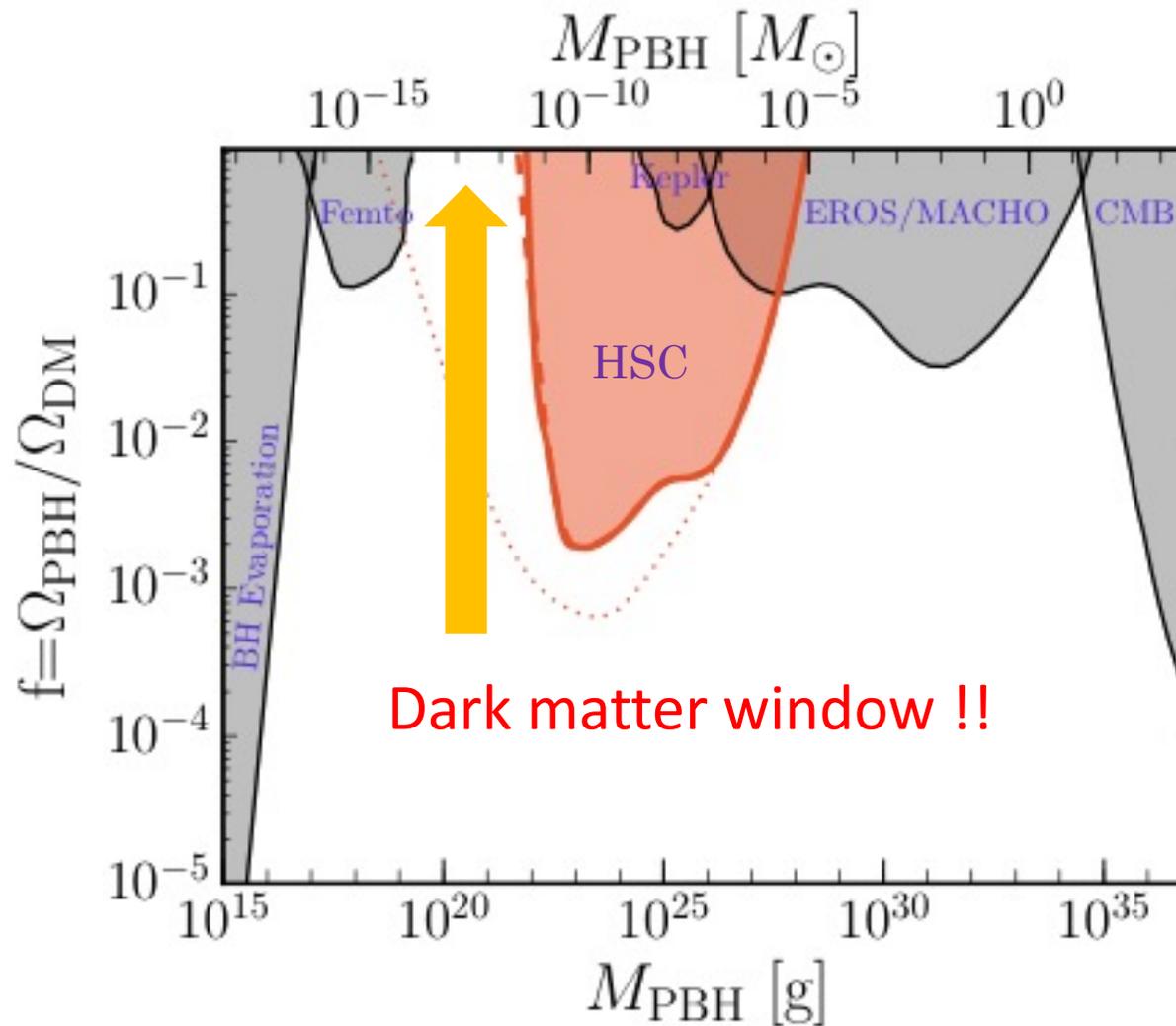


$$M = \gamma M_{\text{PH}} = \frac{4\pi}{3} \gamma \rho H^{-3} \approx 2.03 \times 10^5 \gamma \left(\frac{t}{1 \text{ s}} \right) M_{\odot}.$$

$$t \approx 0.738 \left(\frac{g^*}{10.75} \right)^{-1/2} \left(\frac{T}{1 \text{ MeV}} \right)^{-2} \text{ s},$$

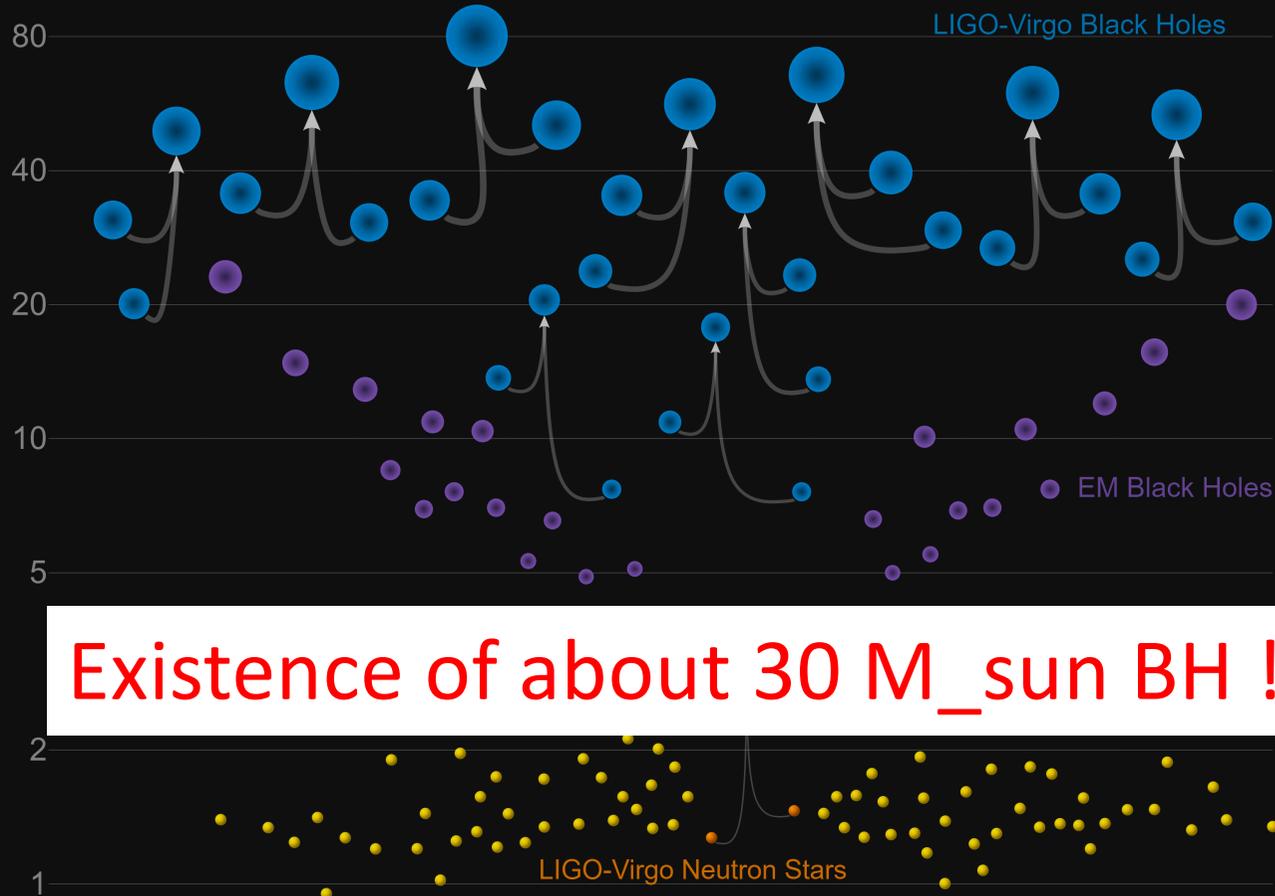
$$30 M_{\odot} \leftrightarrow 70 \text{ MeV}$$

“Conservative” constraints



10 BH-BH merger events and 1 NS-NS

Masses in the Stellar Graveyard *in Solar Masses*



©LIGO/VIRGO collaboration

LIGO-Virgo | Frank Elavsky | Northwestern

OGLE-IV (data) results -exoplanet search -

OGLE (Optical Gravitational Lensing Experiment) IV;

Udalski, Szymanski, Szymanski, 1504.05966

5-years monitoring observations of stars in the Galactic bulge

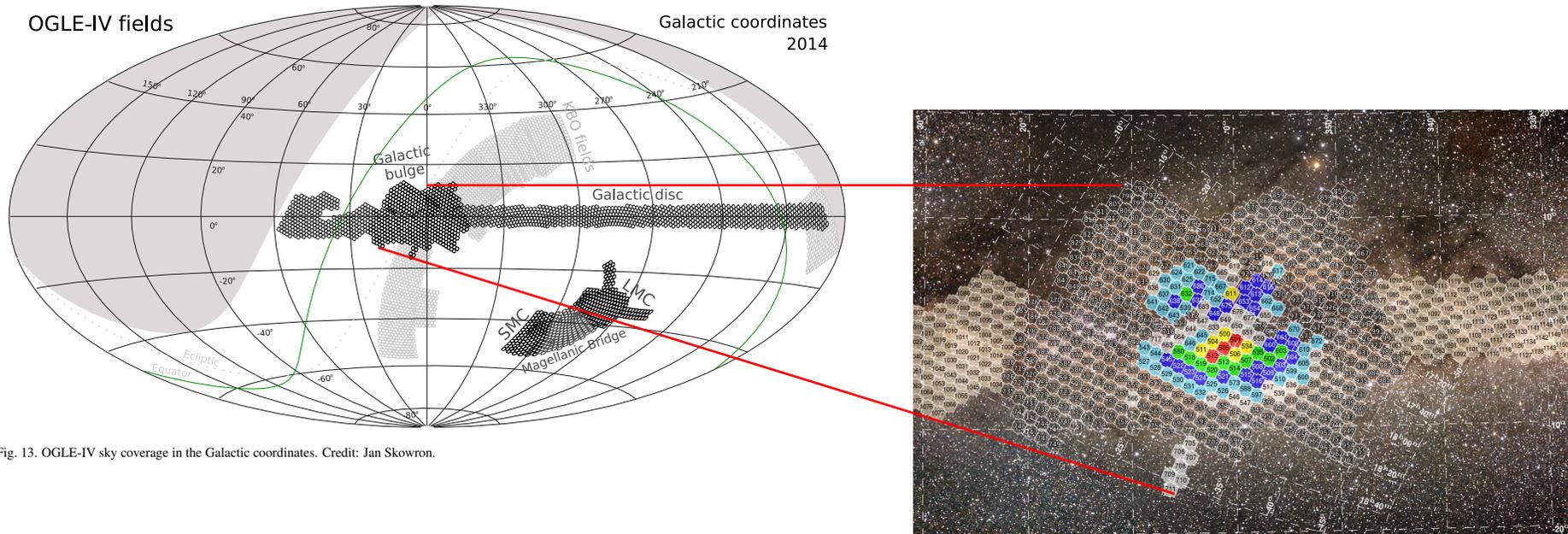
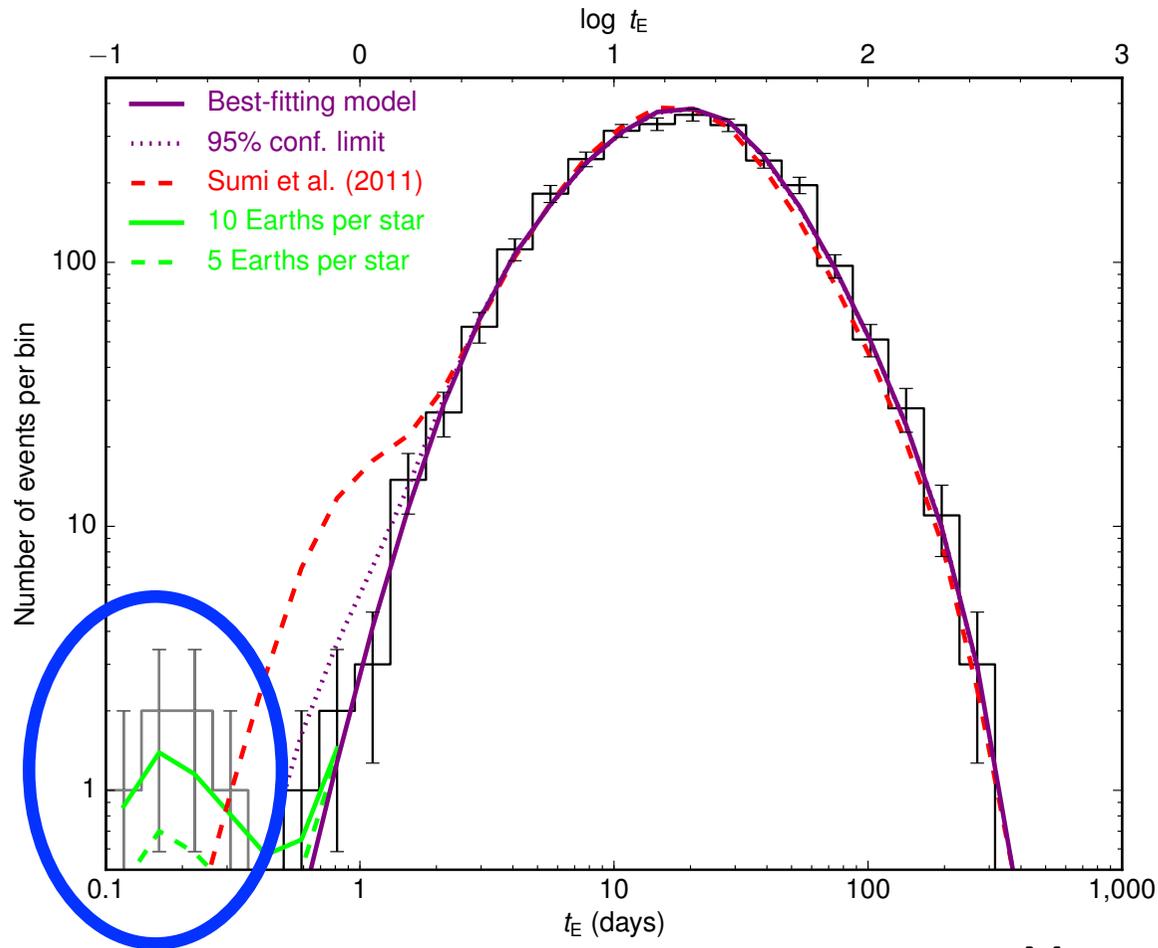


Fig. 13. OGLE-IV sky coverage in the Galactic coordinates. Credit: Jan Skowron.

Earth-mass PBHs???

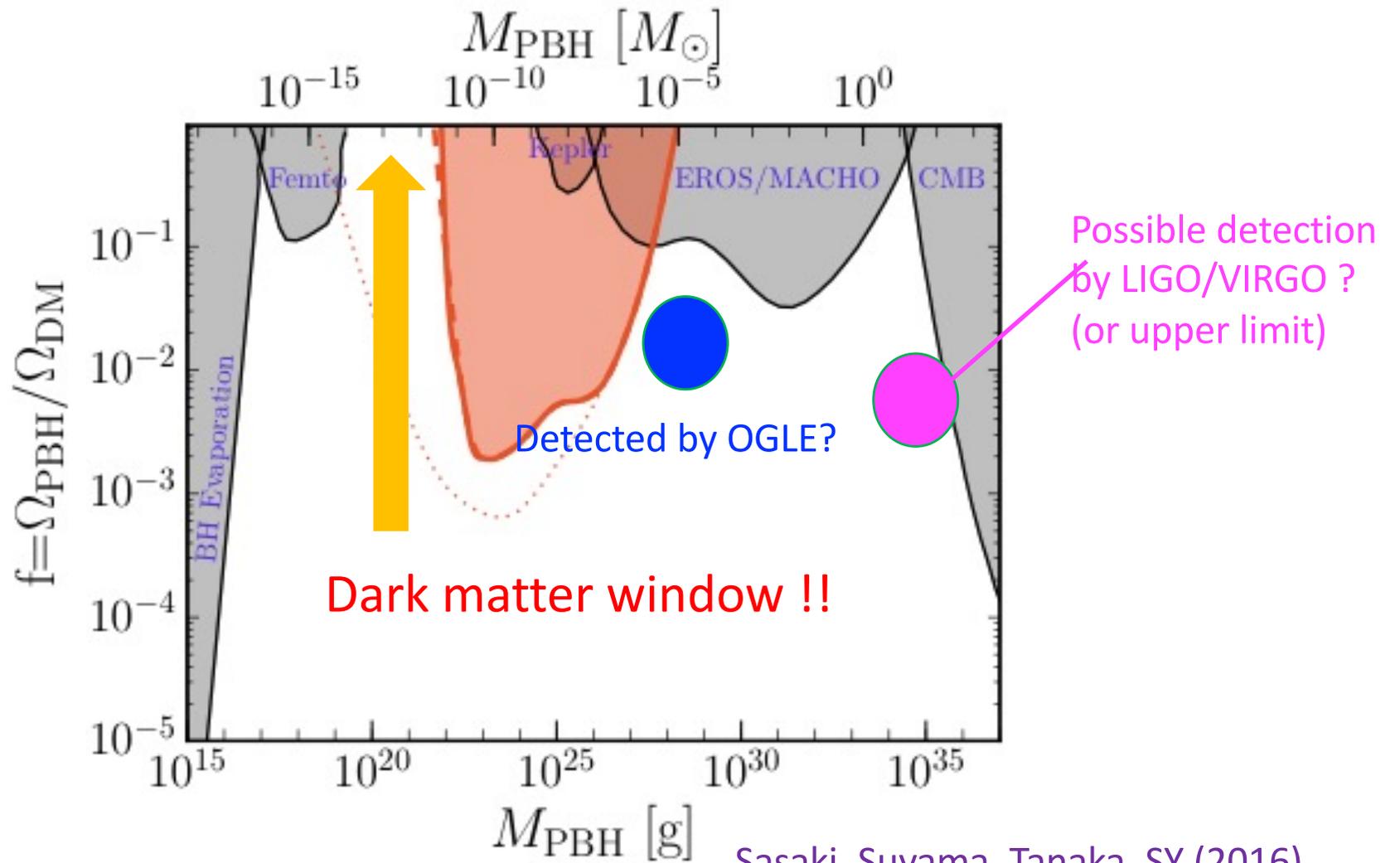


Mroz et al. arXiv:1707.07634

6 microlensing events with short-time scale

→ detection of earth mass PBHs?

Earth mass BHs, LIGO BHs and DM



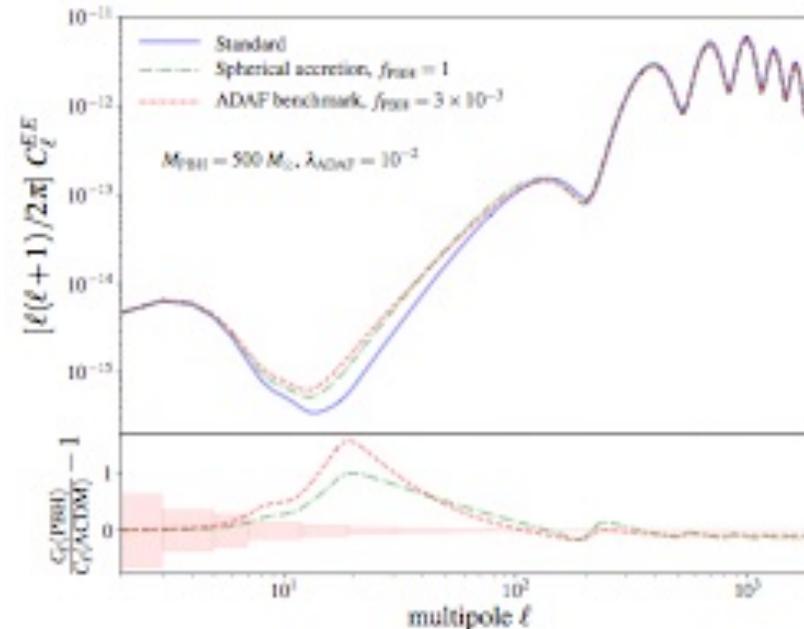
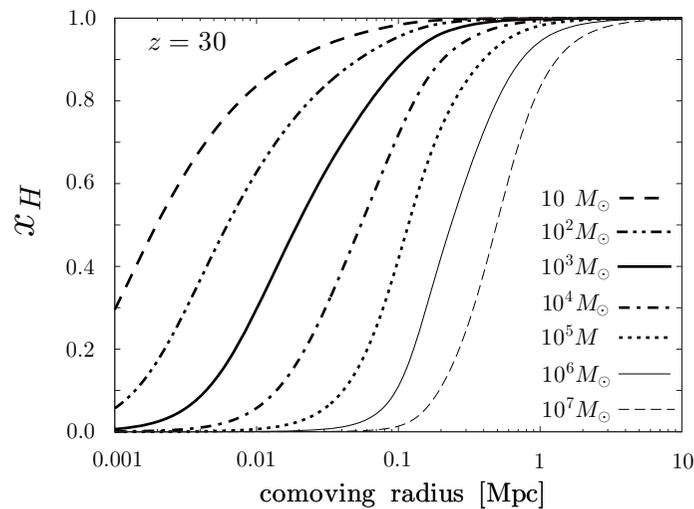
Sasaki, Suyama, Tanaka, SY (2016),
Niikura, Takada, SY, Sumi, Masaki (2019)

Can we probe PBH-DM by SKA?

- SKA as a probe of high redshift Universe

➤ Tashiro and Sugiyama (2012), and more.. (e.g., Poulin et al. (2017), ...)

X-ray photons emitted by accretion of matter onto PBHs



change the optical depth

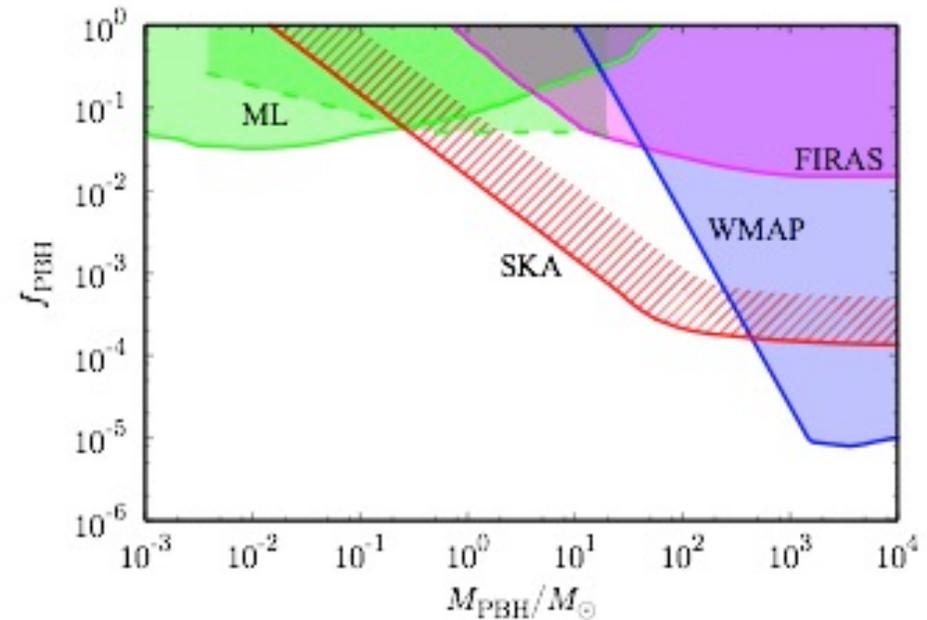
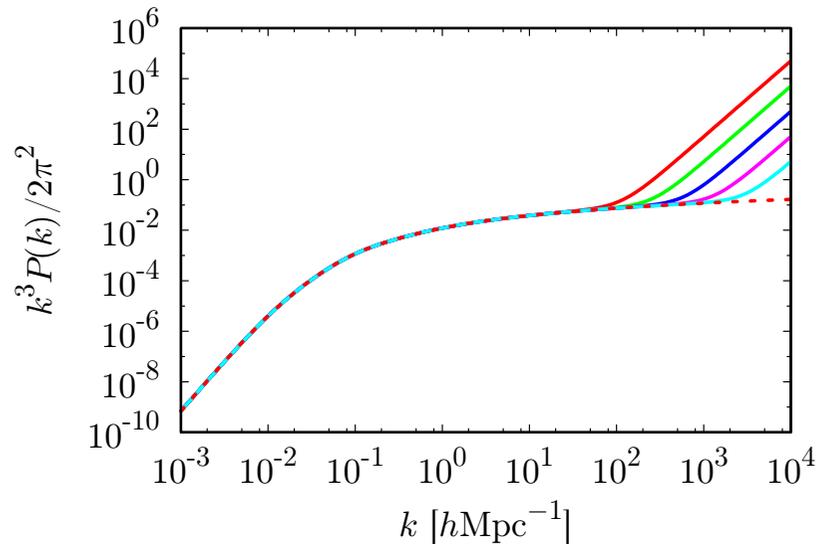
Can we probe PBH-DM by SKA?

- SKA as a probe of high redshift Universe

 - Gong and Kitajima (2017)

Poisson like isocurvature fluctuations of PBHs

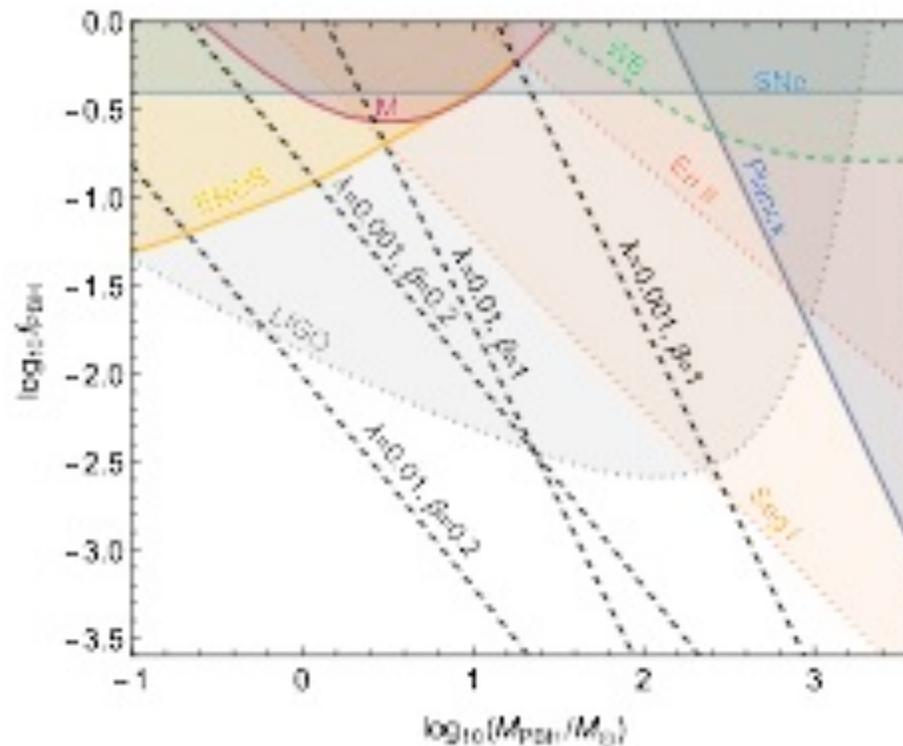
Matter power spectrum



Can we probe PBH-DM by SKA?

- SKA as a probe of high redshift Universe

From EDGES result ...

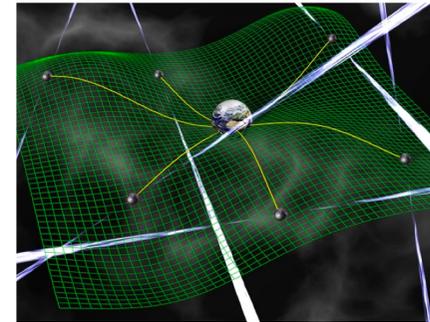


depending on
the astrophysical parameters
(accretion rate, ...)..

Hektor et al. (2018)

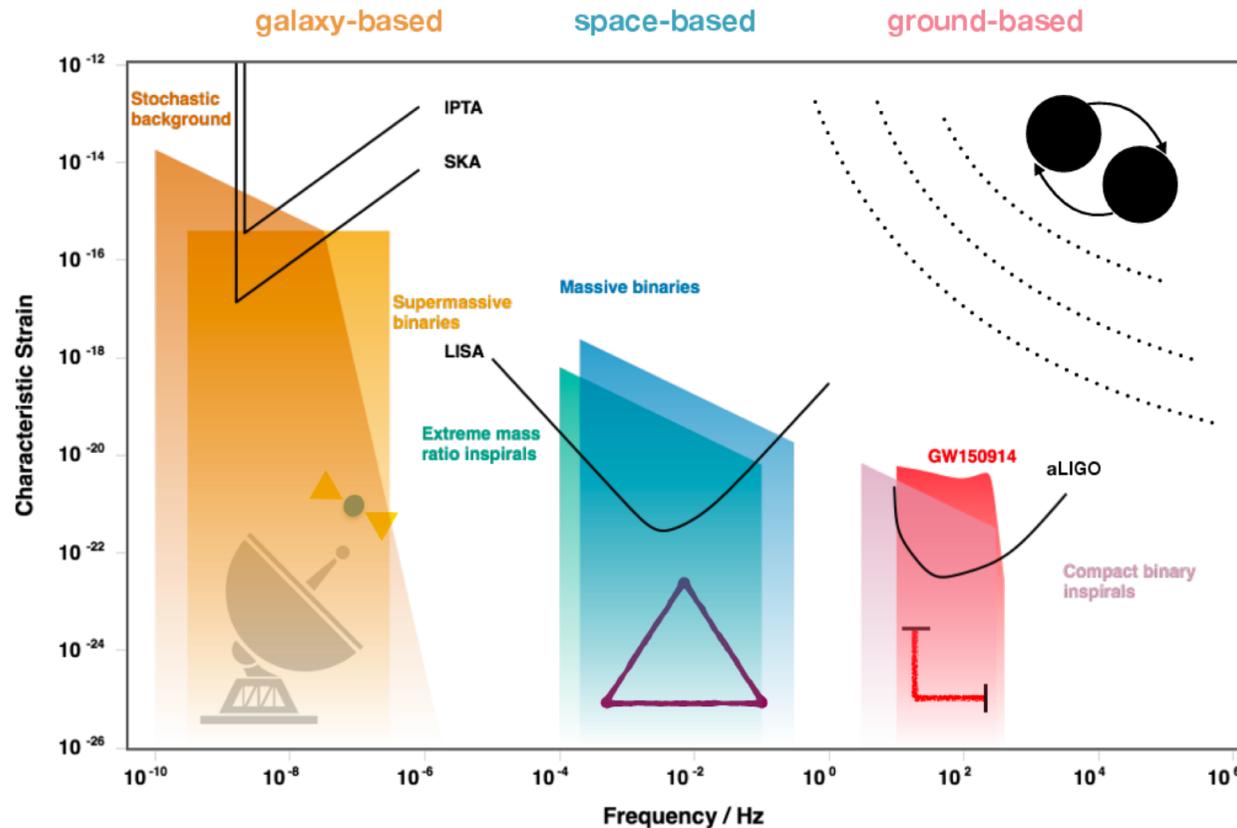
Can we probe PBH-DM by SKA?

- SKA as a PTA



Pulsar Timing Array is known to be an GW detection experiment.

SKA can find lots of radio Pulsars!



Barak, et al. (2018)

Can we probe PBH-DM by SKA?

See, e.g. Saito and J. Yokoyama (2009)

Density fluctuations with large amplitude → collapse → PBH formation



Based on the cosmological perturbation **up to the second order,**



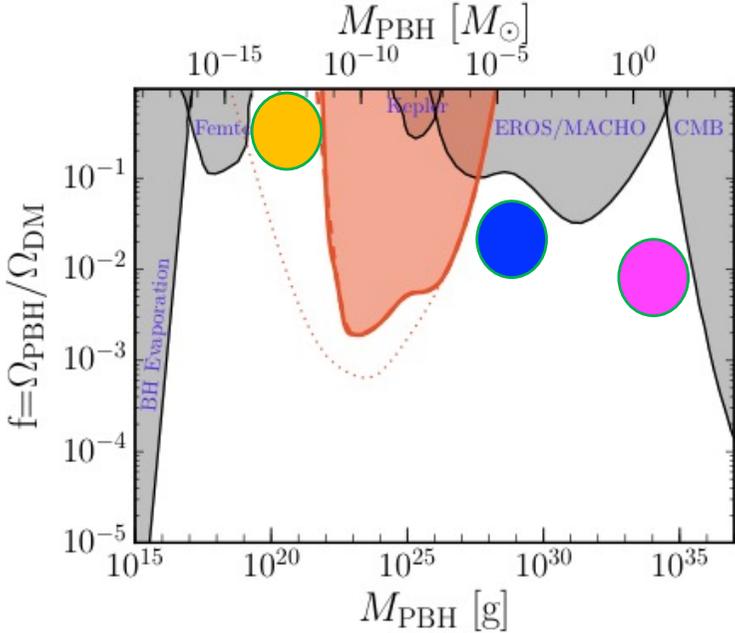
Density fluctuations would be source of the tensor modes, that is, gravitational waves!!

frequency (wave number) of induced GWs \sim horizon scale at the reenter

mass of PBH \sim horizon mass at the reenter

Can we probe PBH-DM by SKA?

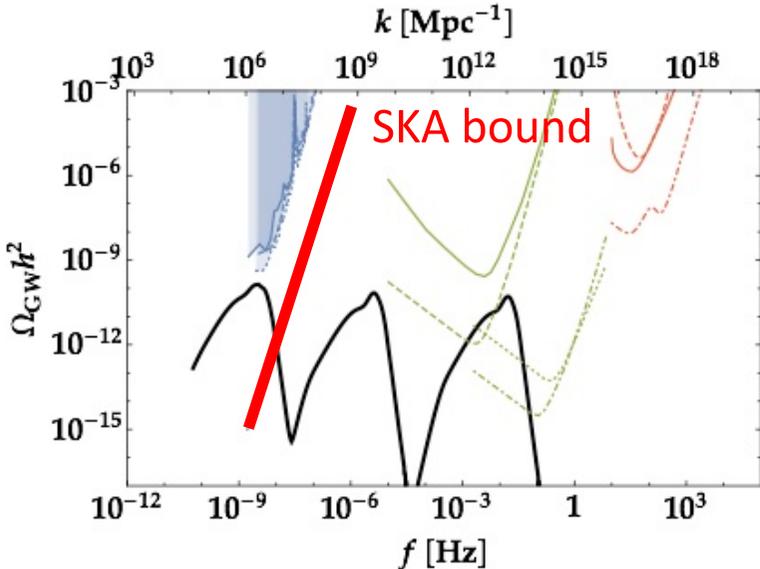
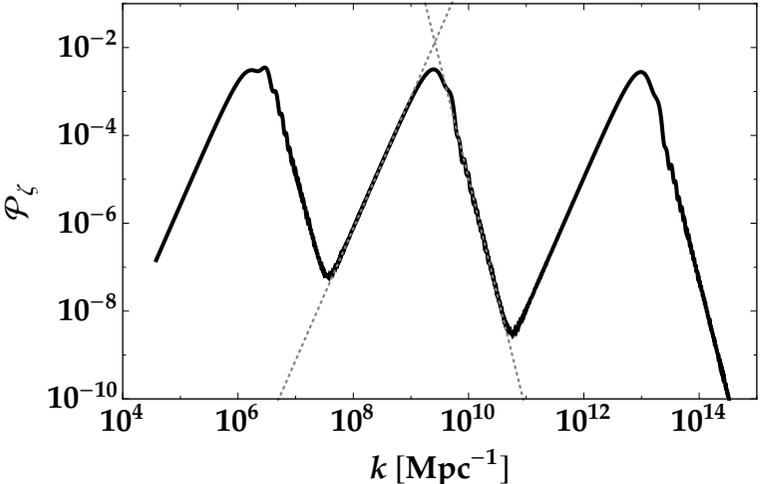
- SKA as a PTA



induced GWB

Tada, SY in prep.

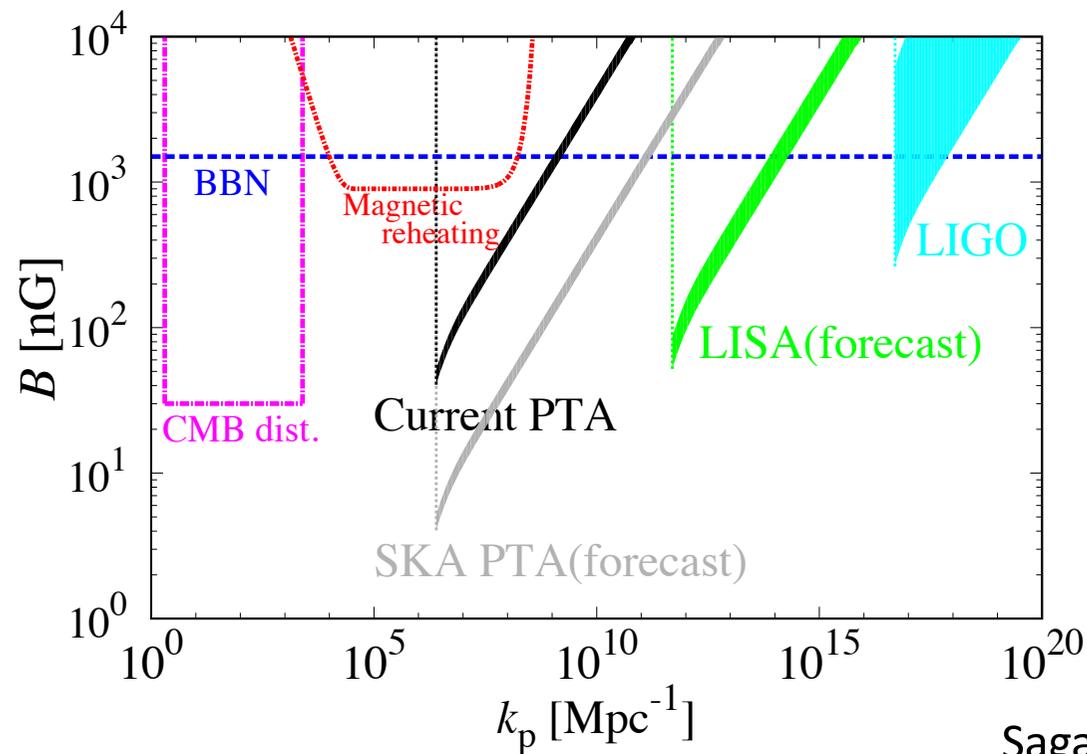
Primordial scalar power



byproduct

- SKA as a PTA

Primordial magnetic field x primordial magnetic field → primordial GWs



Saga, Tashiro, SY (2018)

summary

Observational inflation cosmology

SKA

- Higher order

$$\sigma(f_{\text{NL}}) = 0.61 \text{ (0.50)}$$

- Smaller scales

	$10^{-3}\Delta n_s$	$10^{-3}\Delta\alpha_s$	$10^{-3}\Delta\beta_s$
Planck	7.7	10.7	15.1
COrE	3.2	2.9	6.5
SKA	4.6	2.9	1.5
FFTT	2.4	1.6	0.79
Planck+SKA	1.7	2.0	0.63
Planck+FFTT	1.3	1.3	0.44
COrE+SKA	1.2	1.6	0.39
COrE+FFTT	0.95	1.1	0.28

And more;

- 21cm global signal (small scale structure → gas temp. evo., ...) [Yoshiura, Takahashi² \(2018\)](#)
- 21cm lensing (detecting PGWs) [Book, Kamionkowski, Schmidt \(2011\)](#)

$$r \sim 10^{-9}$$

What is DE?

SKA

- Points for observations

- ✓ Cosmological constant

$$\Delta w < 0.05$$

- ✓ Quintessence models – thawing type

$$\Delta(dw/dt) < 0.1$$

- freezing type

- ✓ Scalar-tensor theories – Horndeski, DHOST theories,...

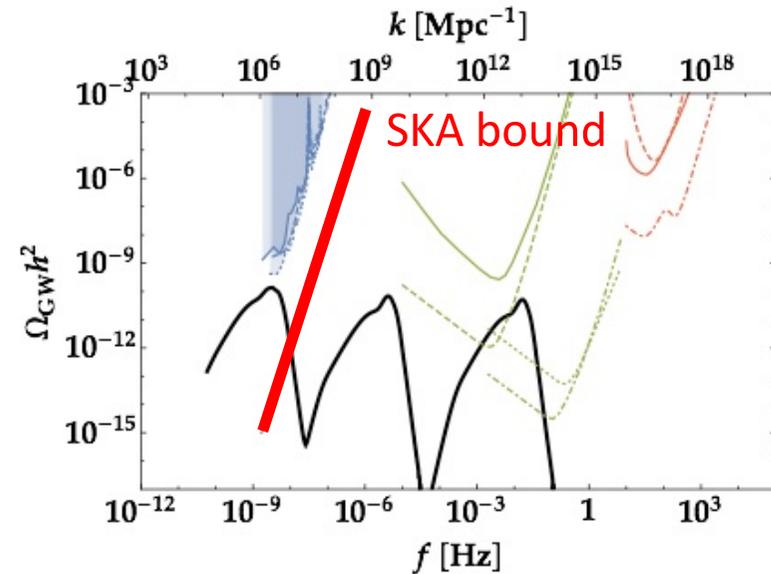
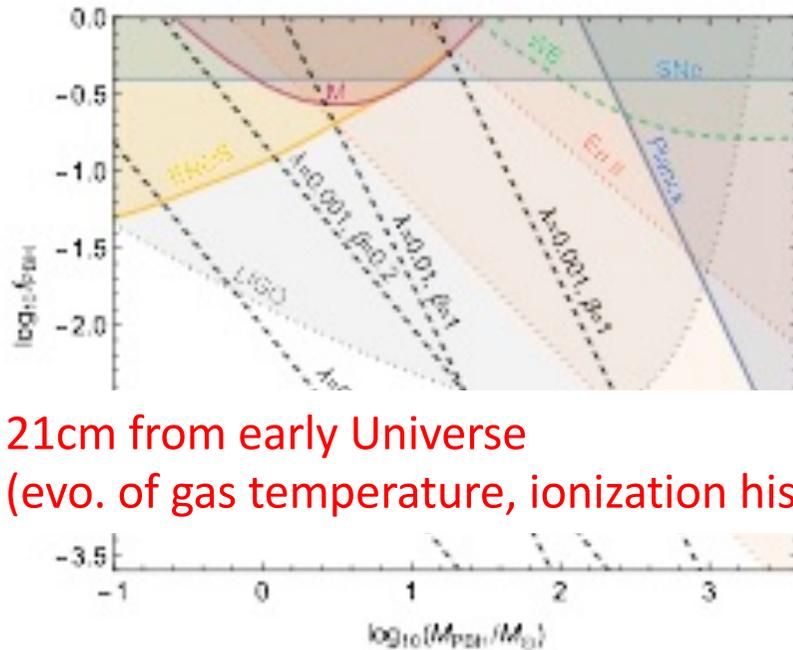
$$\Delta\gamma < 0.02$$

And more;

- DE constraints from early Universe [Kohri et al. \(2016\)](#)
- growth index, or MG in astrophysical bodies, in early Universe?

Can we probe DM by SKA?

- PBH-DM



And more;

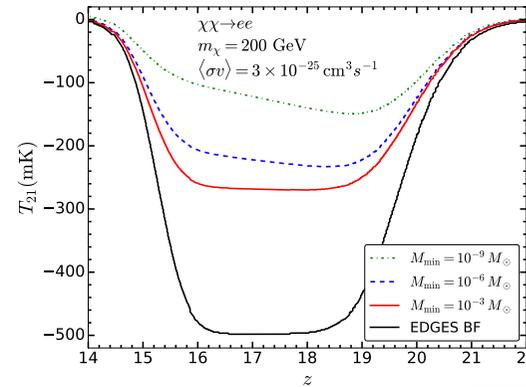
- small scale DM clumps with PTA [Oguri, Kashiyama \(2018\)](#)
- any other idea? microlensing, radio sources, ...

Can we probe other DM by SKA?

- Baryon – DM interaction**

evolution of gas temperature

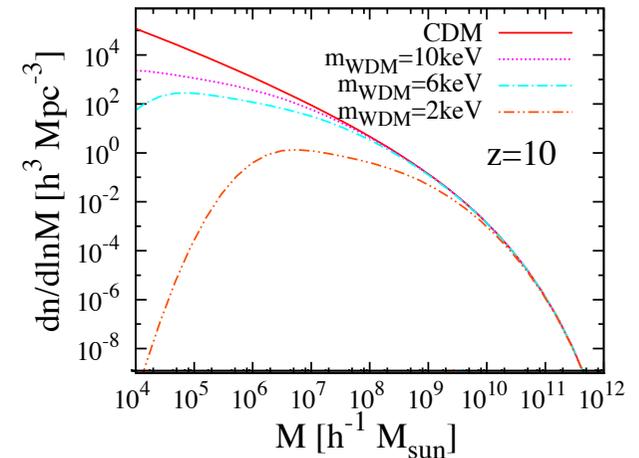
Fialkov, Barkana, Cohen (2018),
 Cheung et al. (2018),
 Kovetz et al. (2018), ...



- Warm DM**

SKA as a probe of small scale structure

Shimabukuro, Inoue, Ichiki, SY (2014),
 Sekiguchi, Tashiro (2014),



- Axion DM** (Ultra light particles, ..)

Axion-photon conversion search
 Kelley, Quinn (2017)

Modulation of grav. potential

Khmelnitsky, Rubakov (2014)

